

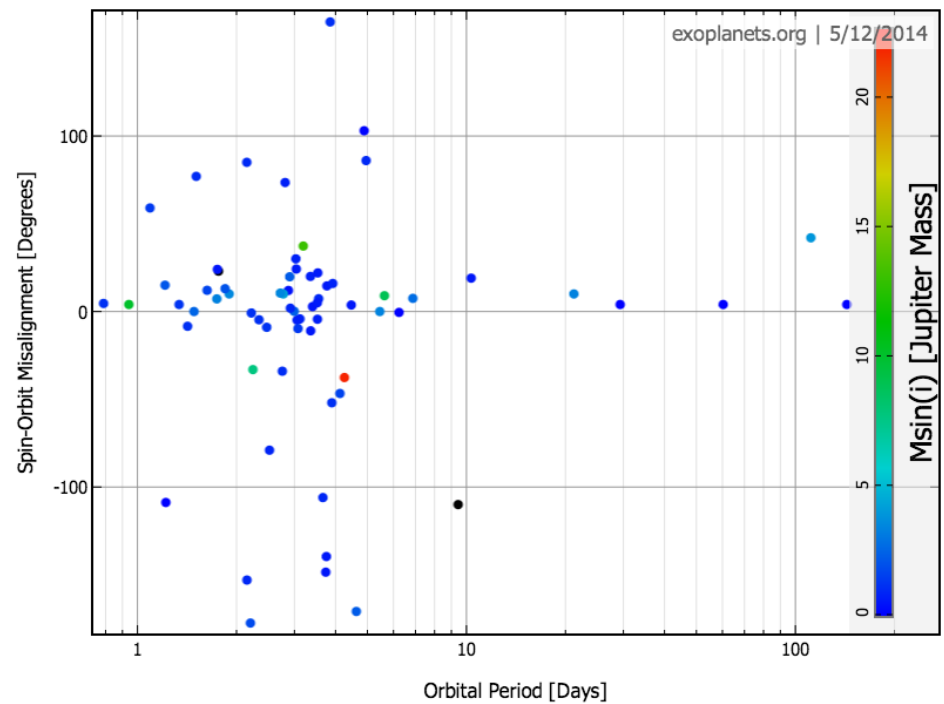
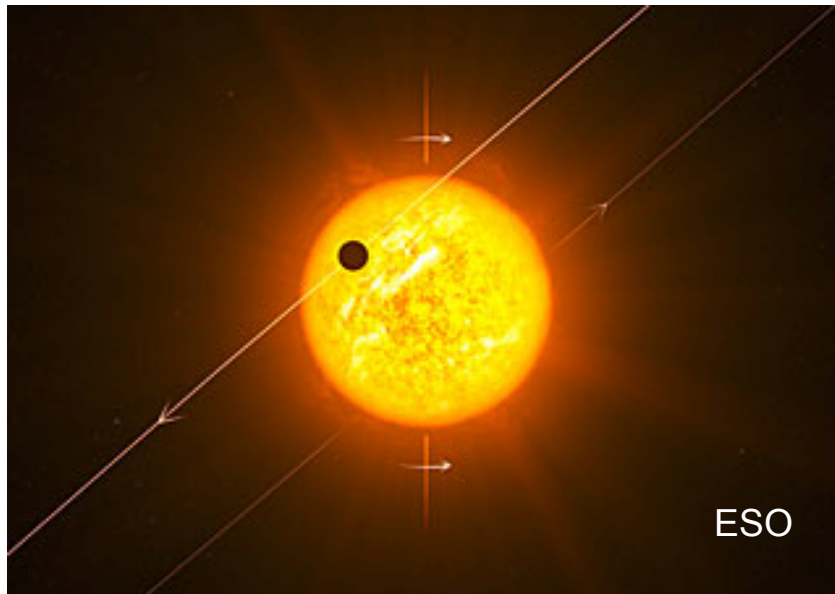
Chaotic Dynamics of Stellar Spin in Binaries and the Production of Misaligned Hot Jupiters

Natalia Storch, Kassandra Anderson & Dong Lai

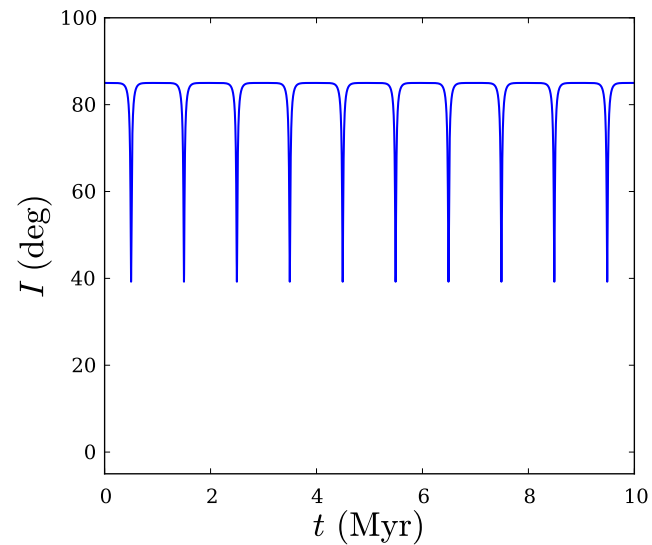
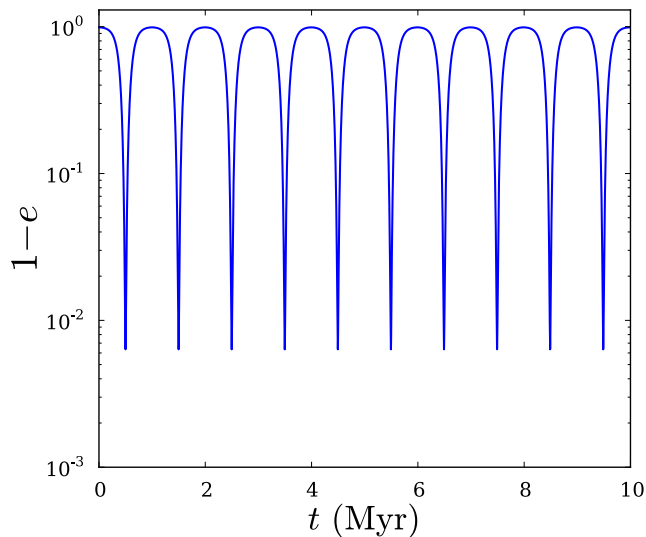
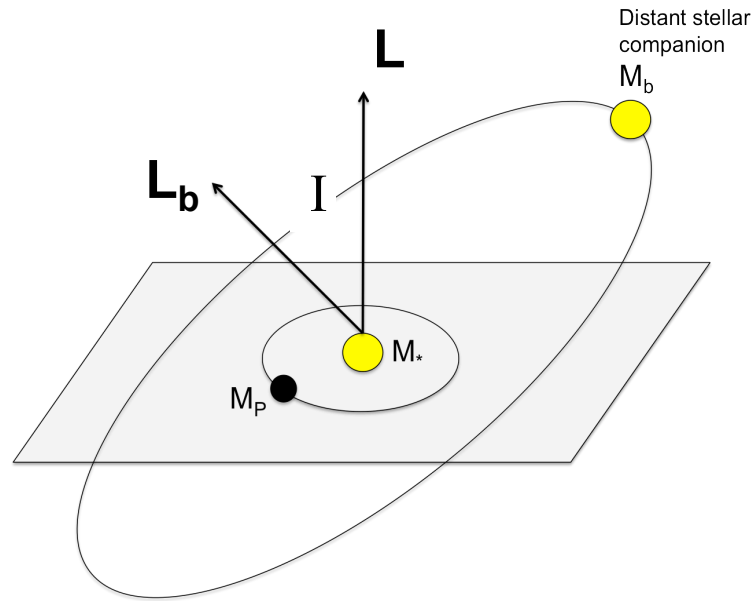
Cornell University



Many hot Jupiter systems have been found to exhibit misalignment between the orbital axis (\mathbf{L} , the axis perpendicular to the orbital plane) and the rotation axis (\mathbf{S}) of its host star



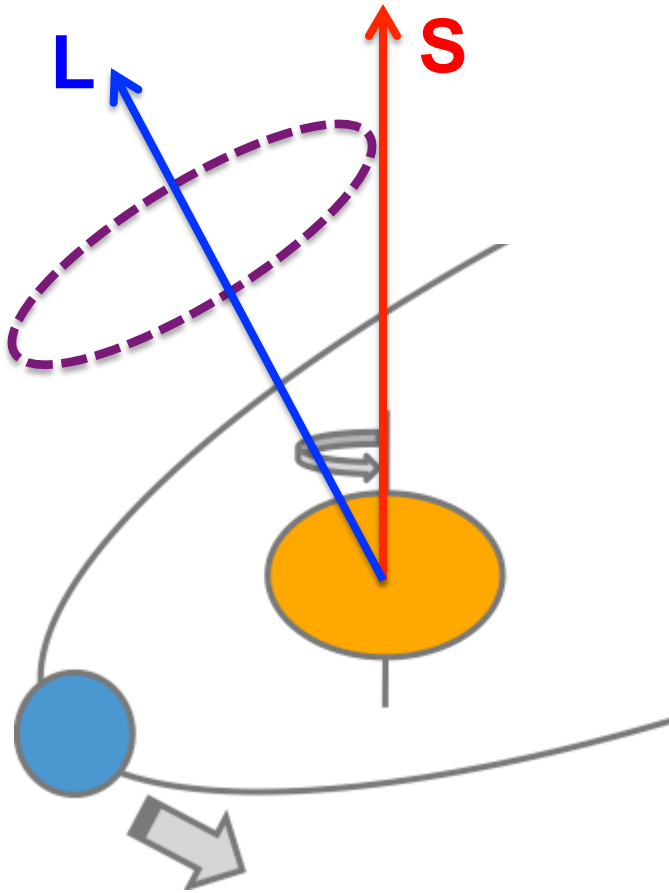
A distant (~ 100 AU) binary companion (M_b) of the planet-hosting star (M_*) can change the eccentricity (e) and inclination (I , the angle between \mathbf{L} and the binary axis \mathbf{L}_b) of the planet (M_p) in a periodic way -- This is called Kozai-Lidov oscillation



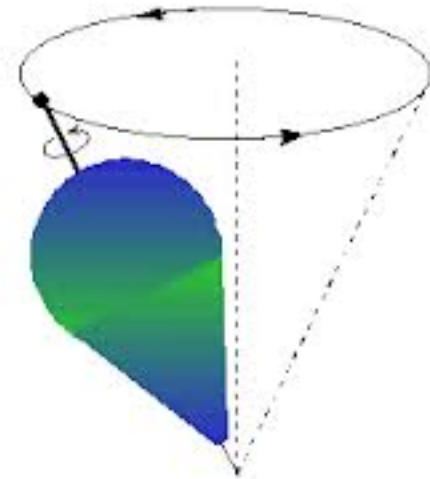
Stellar Spin Dance

The host star is spinning, and therefore has an oblate shape.

Gravity from the planet acting on the oblate star makes **S** (the rotation axis of the star) precess around **L** (the orbital axis of the planet).



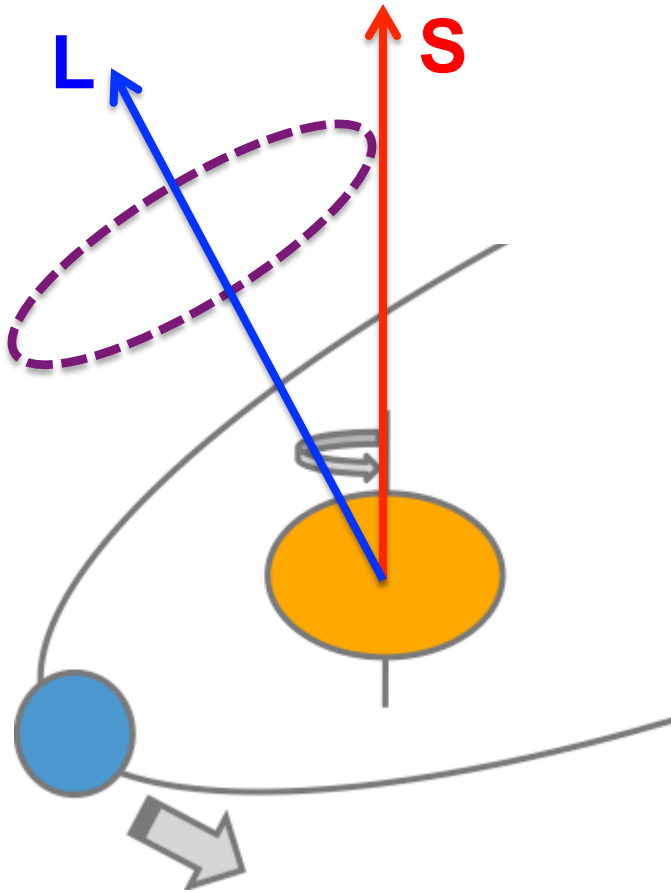
This is analogous to the precession of a spinning top due to Earth's gravity



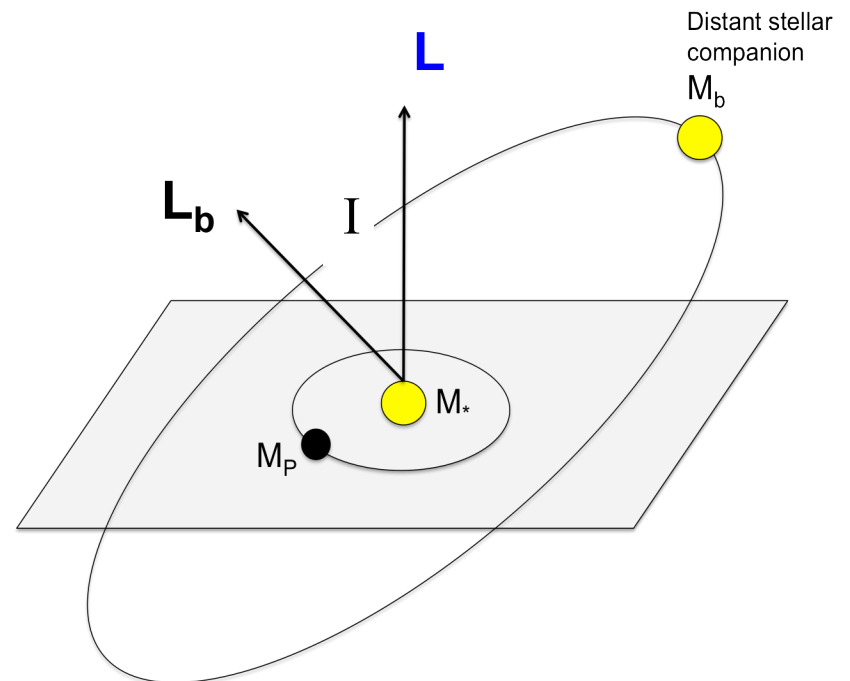
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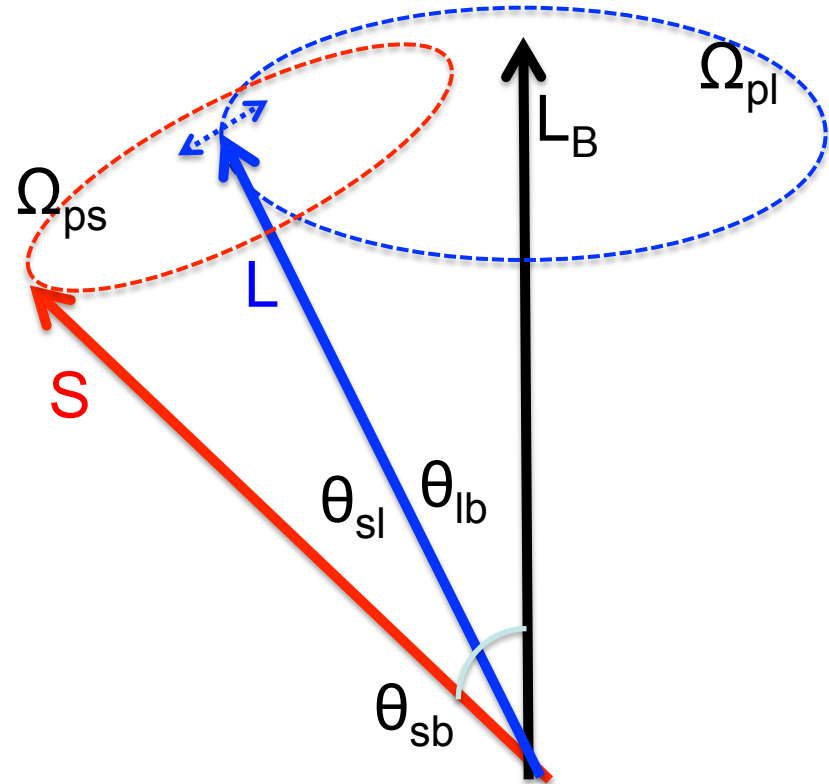
However, recall that \mathbf{L} itself is changing due to the gravity from the distant binary companion



Spin-Orbit Evolution

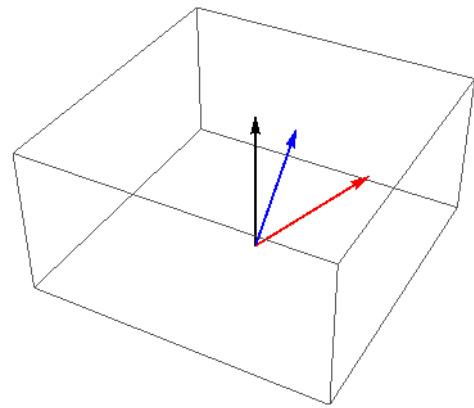
So we have:

- **L** moves around **L_B** (the orbital axis of the binary, which is not changing) at frequency Ω_{pl}
- **S** moves around **L** at frequency Ω_{ps}



This coupled motion of **S** and **L** gives rise to complex (even chaotic) evolution of the star's spin axis and the spin-orbit angle

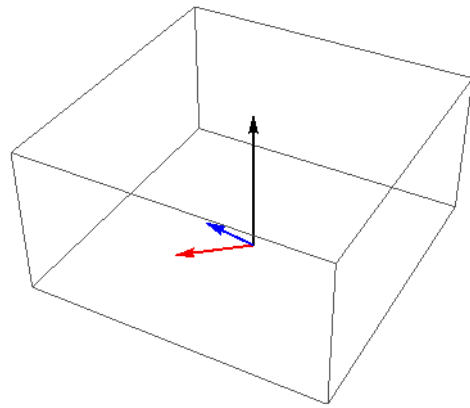
For Ω_{pl} much larger than Ω_{ps} :



— L_B
— L
— S



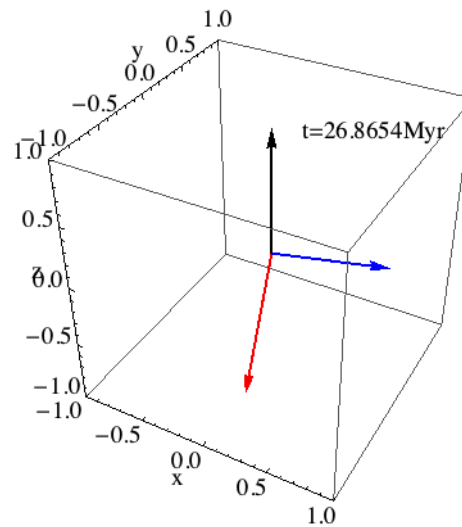
For Ω_{pl} much smaller than Ω_{ps} :



— L_B
— L
— S



For Ω_{pl} comparable to Ω_{ps} :

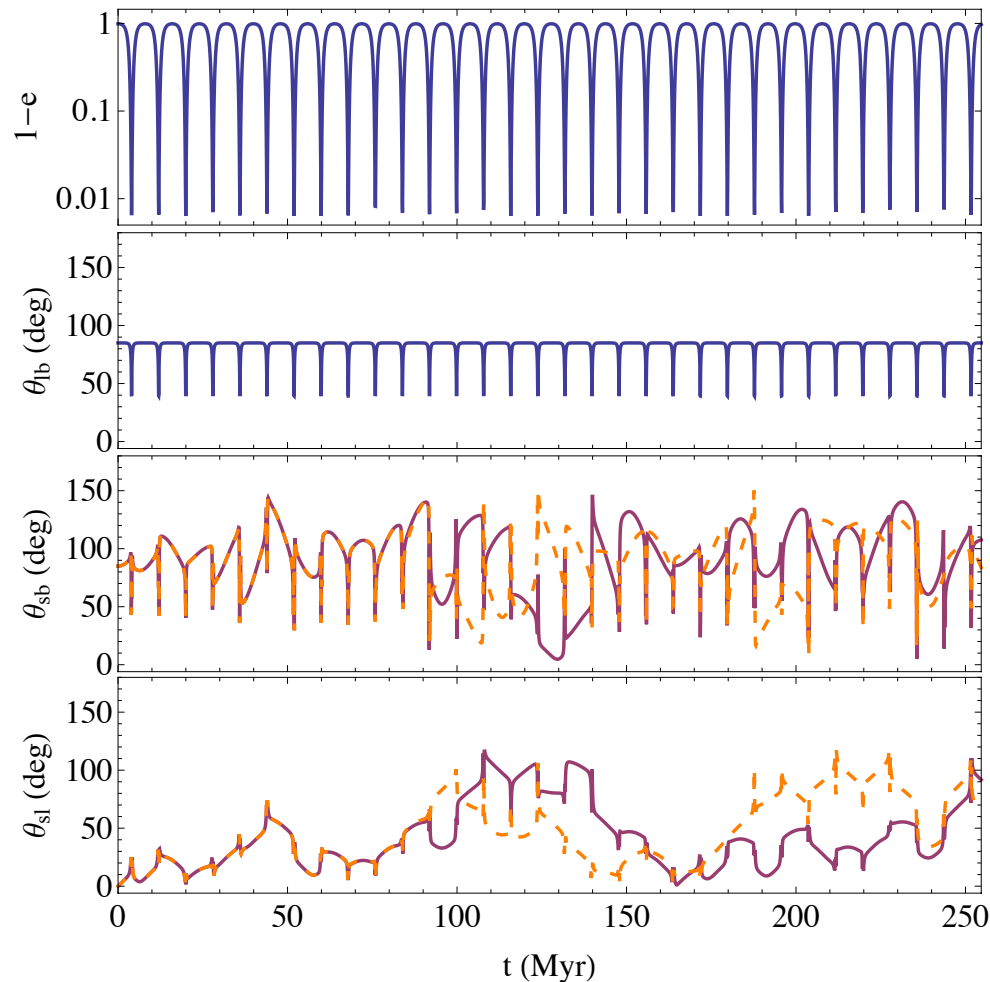


— L_B
— L
— S

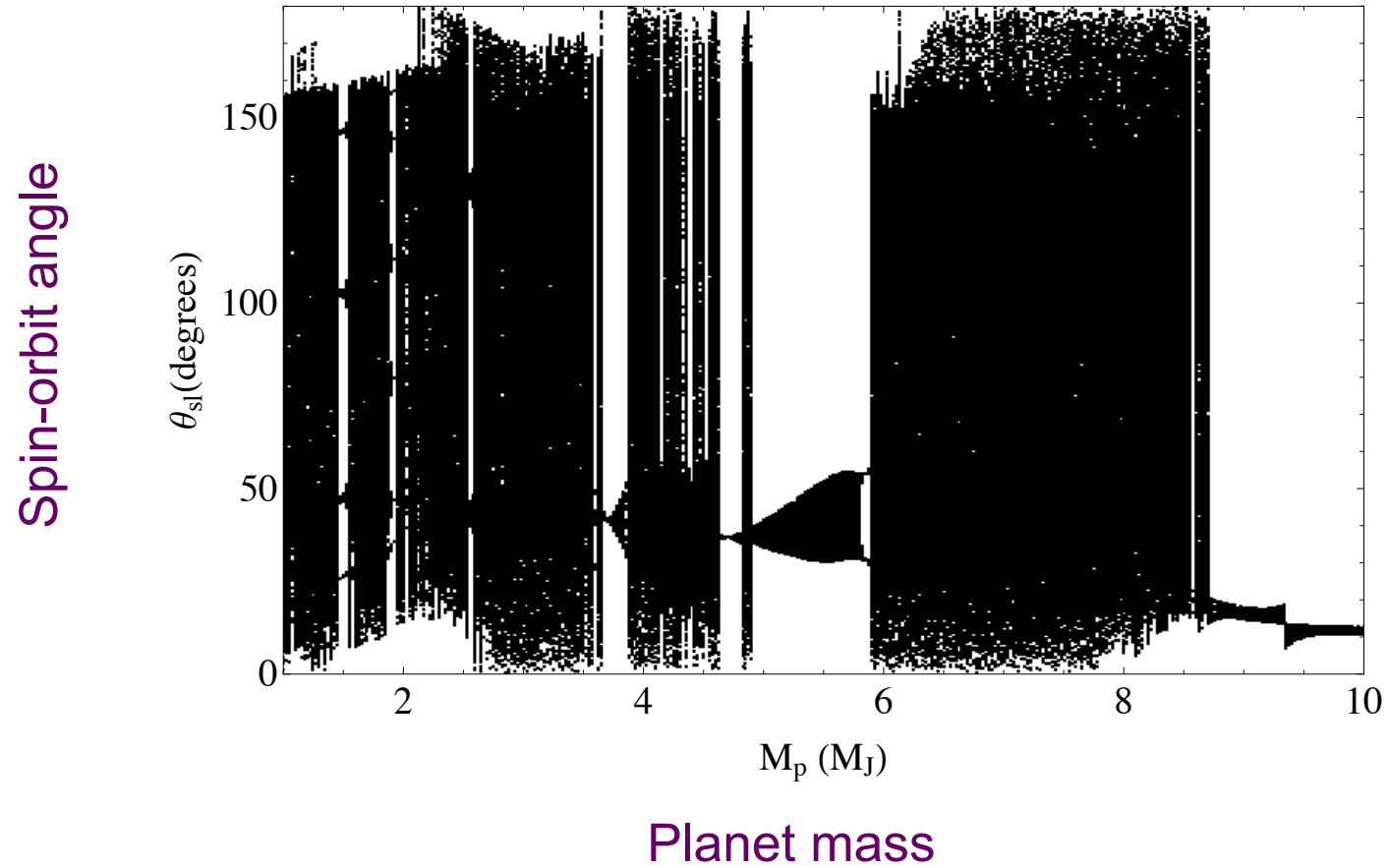


Evolution of Stellar Spin and Planetary Orbit

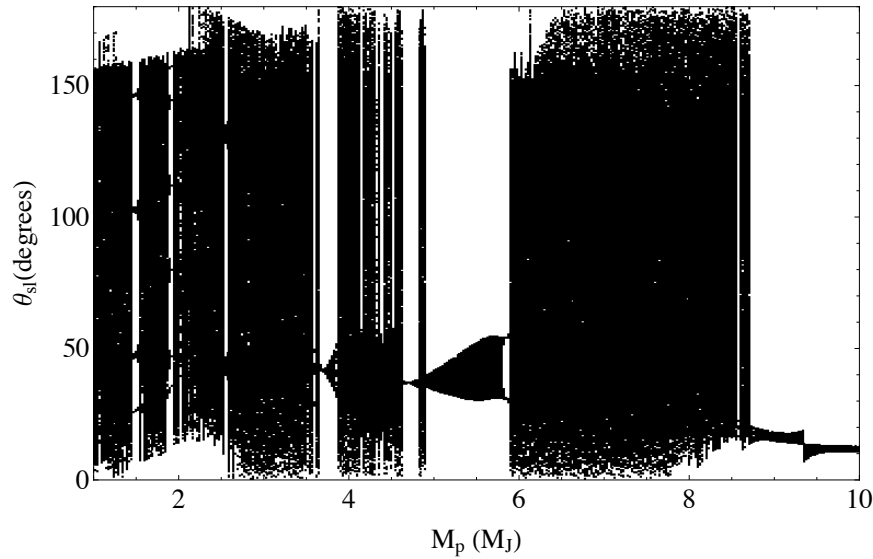
We see that the spin-orbit angle (bottom panel) evolves erratically even when the planet's orbital eccentricity evolves regularly. In fact, the spin evolution can be chaotic: starting from almost the same initial condition, the spin-orbit angles quickly diverge.



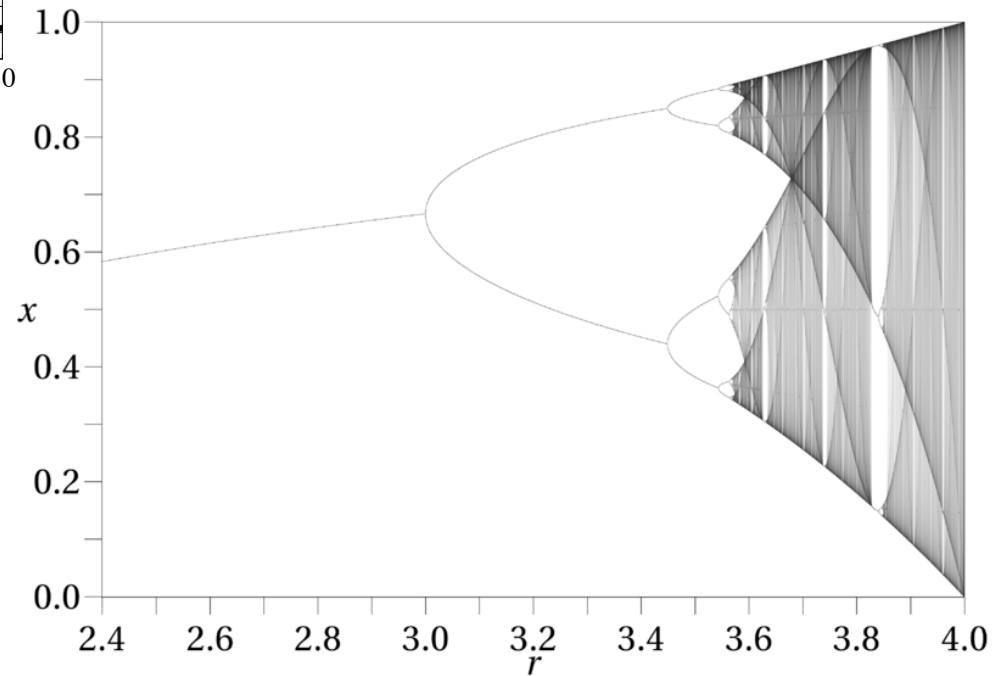
Periodic Islands in a Chaotic Ocean



Periodic Islands in a Chaotic Ocean



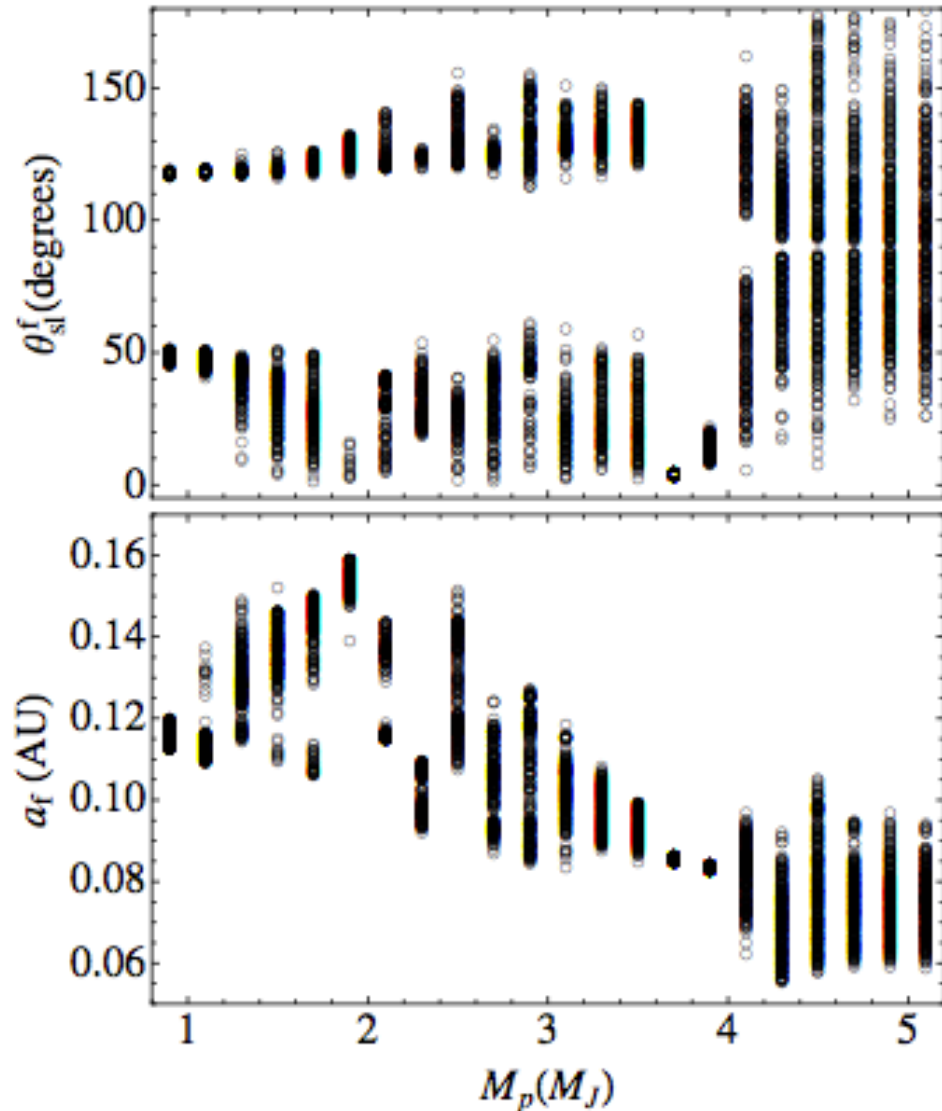
This is analogous to the logistic map:



From wikipedia

Memory of Chaos

A tiny spread in initial conditions can lead to a large spread in the final spin-orbit misalignment



The complex spin evolution can affect the observed distribution of the spin-orbit misalignment angle of hot Jupiter systems.

