

# Highly Magnetized Neutron Stars and Polarized X-Rays

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# Neutron Stars:

## Different Observational Manifestations

- Isolated NSs
- Accreting NSs
- Merging NSs

# Isolated Neutron Stars

Radio pulsars:  $P, \dot{P} \Rightarrow$

Most pulsars :  $B \sim 10^{12-13}$  G

Millisecond pulsars :  $B \sim 10^{8-9}$  G

High – B radio pulsars :  $B \sim 10^{14}$  G

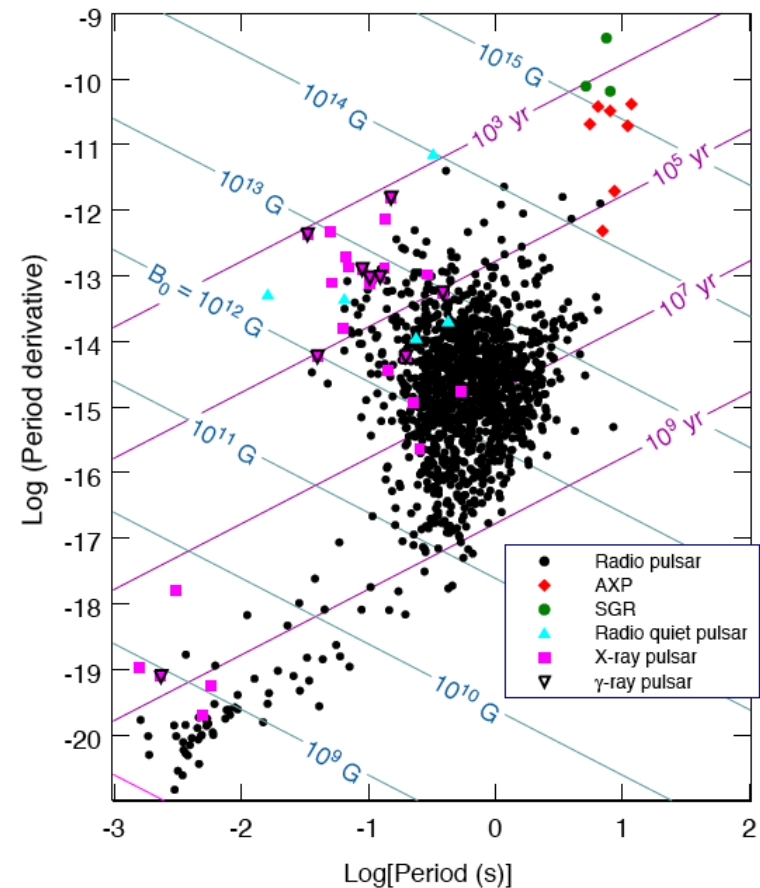
Radiation at all wavelengths:

radio, IR, optical, X-rays, Gamma-rays

New Odd Behaviors:

- RRATs (rotating radio transients)  
radio bursts (2-30 ms), quiescence (min-hrs);  
period  $\sim$  sec
- Intermittent Pulsars (“Sometimes a pulsar”)  
e.g. PSR B1931+24: “on” for  $\sim$  a week,  
“off” for  $\sim$  a month

FRBs??



# Magnetars

Neutron stars powered by superstrong magnetic fields ( $B > 10^{14} \text{G}$ )

Soft Gamma-Ray Repeaters (SGRs) (7+4 systems)

Anomalous X-ray Pulsars (AXPs) (9+3 systems)

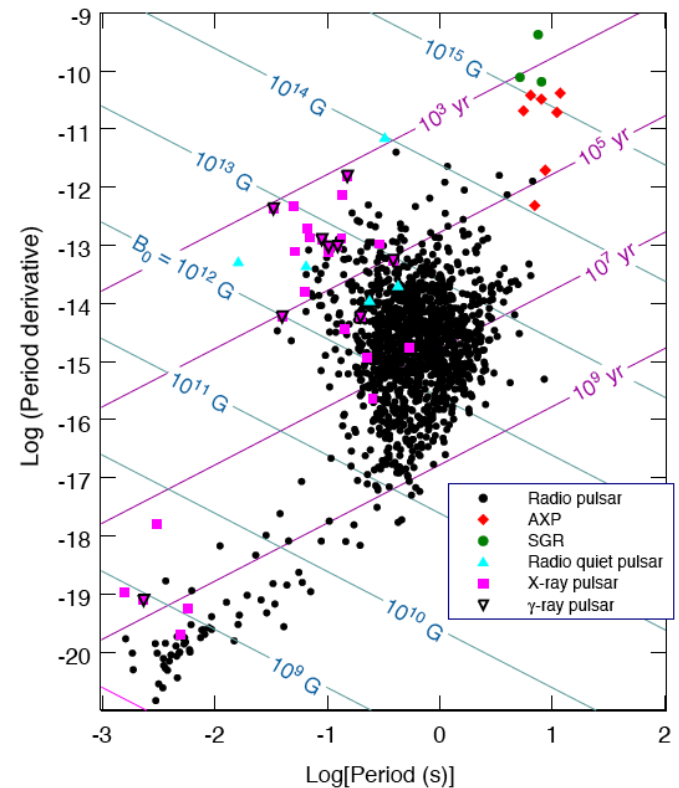
Even in quiescence,  $L \sim 10^{34-36} \text{erg s}^{-1} \gg I\Omega\dot{\Omega}$

AXP/SGR bursts/flares (e.g. Kaspi, Gavriil, Kouveliotou, Woods, etc)

Giant flares in 3 SGRs

12/04 flare of SGR1806-20 has  $E > 10^{46} \text{erg}$

QPOs during giant flares (e.g. Israel, Strohmayer, Watts, etc)



# Thermally Emitting Isolated NSs

“Perfect” X-ray blackbody:

RX J1856.5-3754

Spectral lines detected:

(e.g., van Kerkwijk & Kaplan 06; Haberl 06)

RXJ1308+2127 (0.2-0.3 keV)

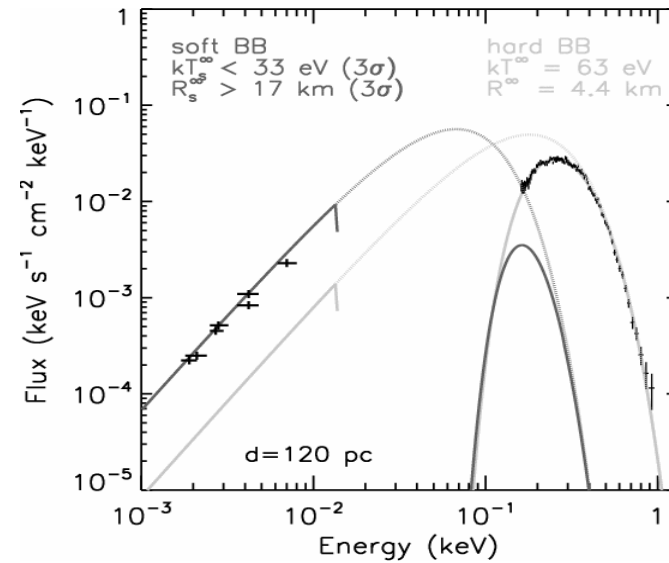
RXJ1605+3249 (~0.45 keV)

RXJ0720-3125 (~0.3 keV)

RXJ0420-5022 (~0.3 keV)?

RXJ0806-4123 (~0.5 keV)?

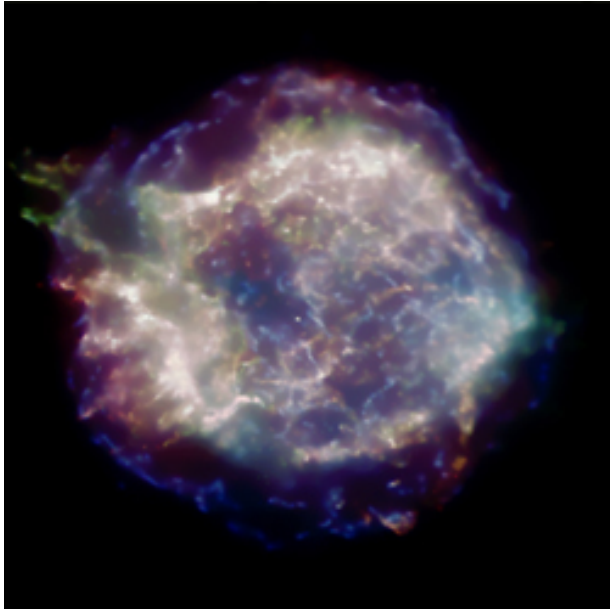
RBS 1774 (~0.7 keV)?



Burwitz et al. (2003)

⇒  $B \sim 10^{13-14}$  G? magnetar descendant & off-beam radio pulsar?

# Central Compact Objects (CCOs) in SNRs



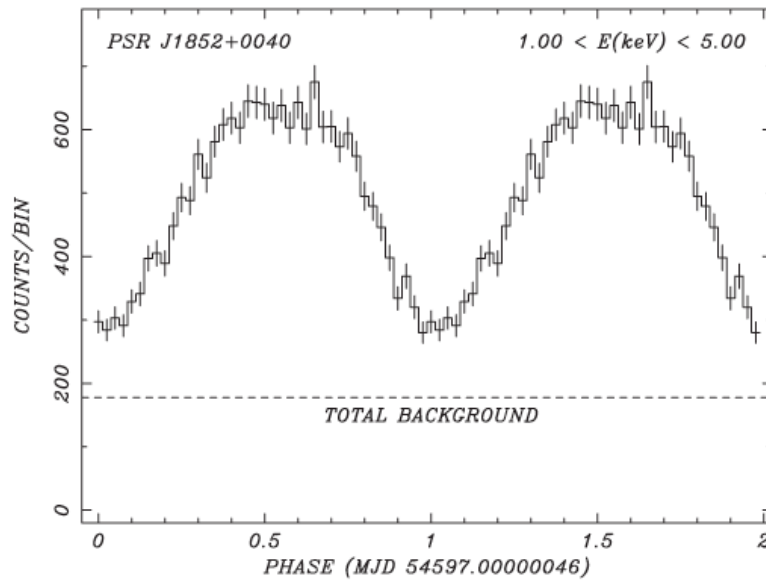
CCO	SNR	Age (kyr)	$d$ (kpc)	$P$ (s)	$f_p^a$ (%)	$B_s$ ( $10^{11}$ G)
RX J0822.0 – 4300	Puppis A	3.7	2.2	0.112	11	<9.8
CXOU J085201.4 – 461753	G266.1 – 1.2	1	1	...	<7	...
1E 1207.4 – 5209	PKS 1209 – 51/52	7	2.2	0.424	9	<3.3
CXOU J160103.1 – 513353	G330.2 + 1.0	$\gtrsim 3$	5	...	<40	...
1WGA J1713.4 – 3949	G347.3 – 0.5	1.6	1.3	...	<7	...
CXOU J185238.6 + 004020	Kes 79	7	7	0.105	64	0.31
CXOU J232327.9 + 584842	Cas A	0.33	3.4	...	<12	...

Halpern & Gotthelf 2010

Small surface dipole field ... (are they “anti-magnetars”?)

# Hidden Magnetic Fields of Neutron Stars

- NS in Kes 79 SNR has  $B_{\text{dipole}} \simeq 3 \times 10^{10}$  G, but large pulse fraction 60%



(Halpern & Gotthelf 2010)

$$\Rightarrow B_{\text{crust}} \sim \text{a few} \times 10^{14} \text{ G}$$

(Shabaltas & DL 2011)

- SGR 0418+5729, with  $B_{\text{dipole}} \simeq 4 \times 10^{12}$  G (Rea et al. 2010)
  - ➔ Internal field is much larger (Turolla et al 2011)

## **Isolated Neutron Stars** (as revealed by X-rays)

- Radio pulsars
- Magnetars
- Other radio-quiet NSs:
  - Central Compact Objects in SNRs
  - “Dim” isolated NSs

## **Future goals:**

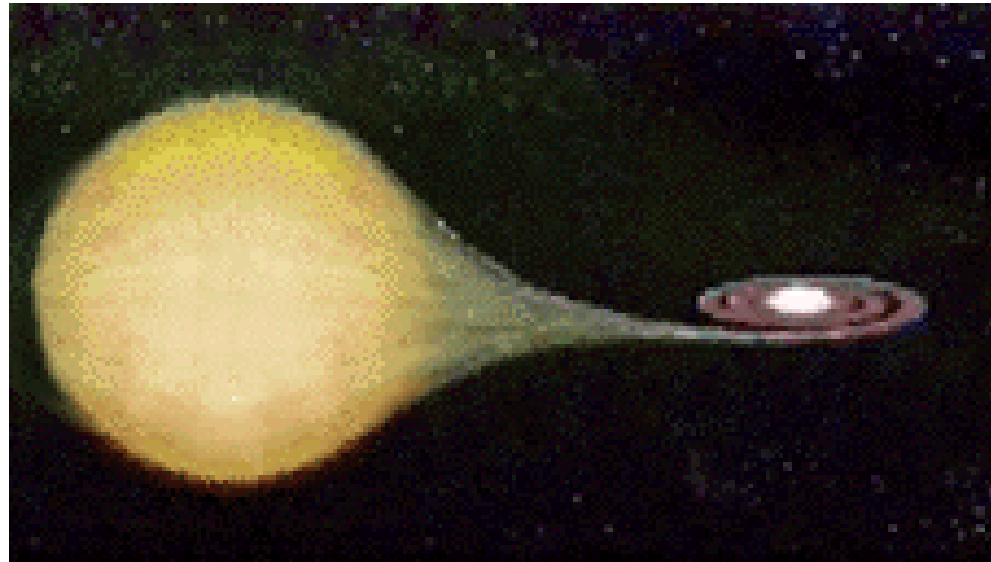
- Understand the evolution and links between different types of NSs
- Understand observed manifestations of these NSs
  - (e.g., Radiative processes in NS atmospheres and magnetospheres)
- Use these NSs to probe physics under extreme conditions
  - (e.g., Strong gravity, high density, and strong B fields)

## **X-ray polarization provides a new window** (in addition to spectra/timing)

Even when spectrum or light curve is boring, polarization can still be interesting

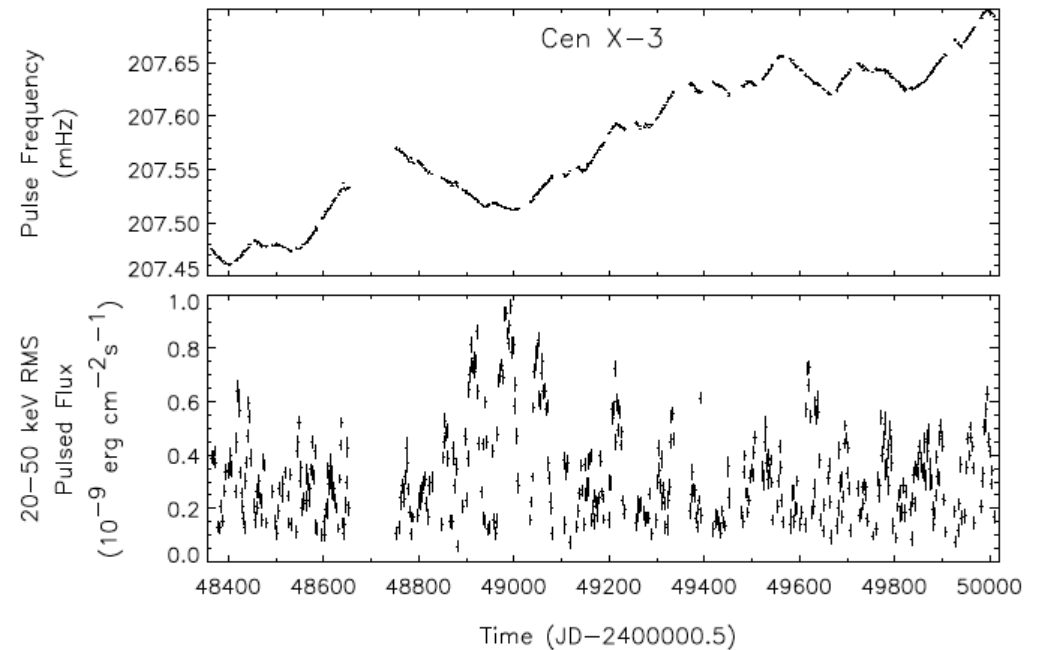
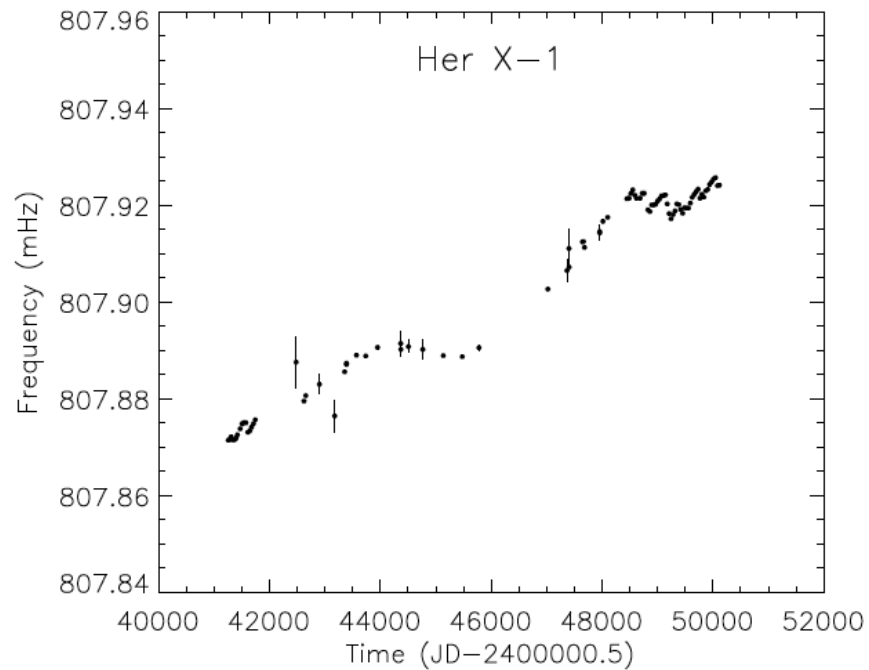


# Accreting Neutron Stars

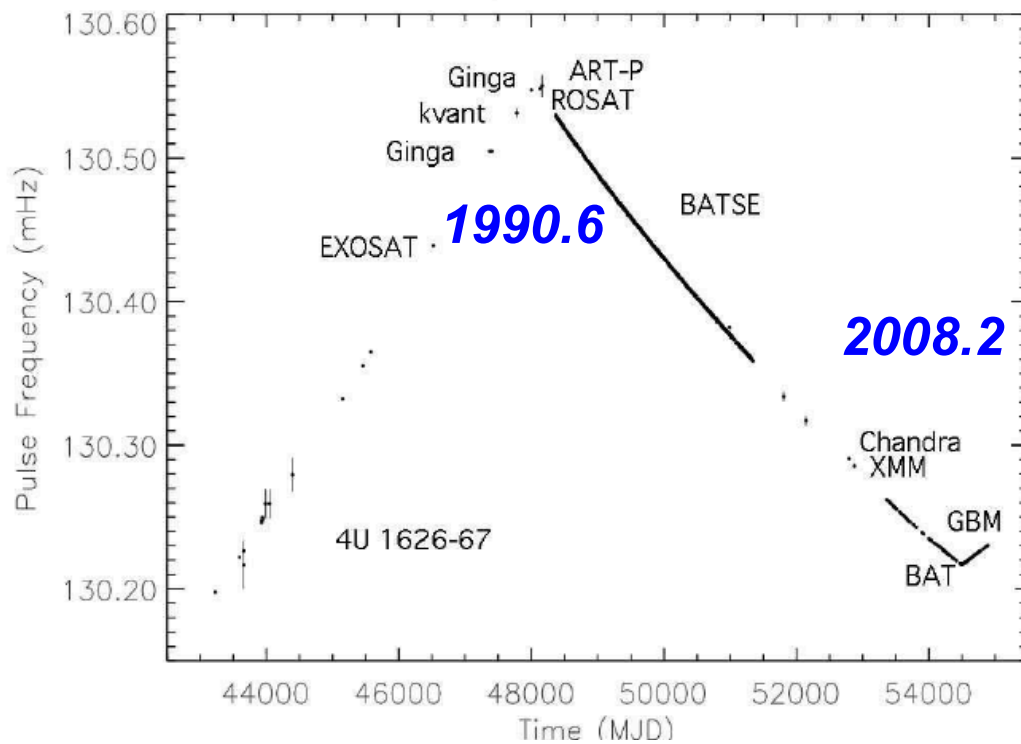


- *Non- or weakly magnetized NSs (LMXBs)*
- *Highly magnetized NSs (HMXBs)*

# Puzzle: Spinup/Spindown of Accreting X-ray pulsars



*Bildsten et al. 1997*

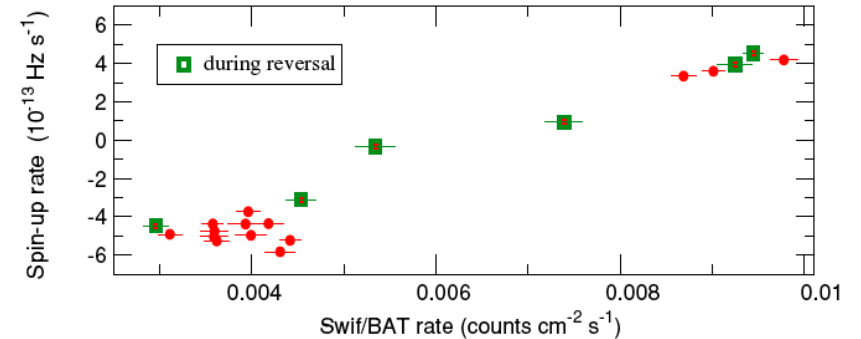
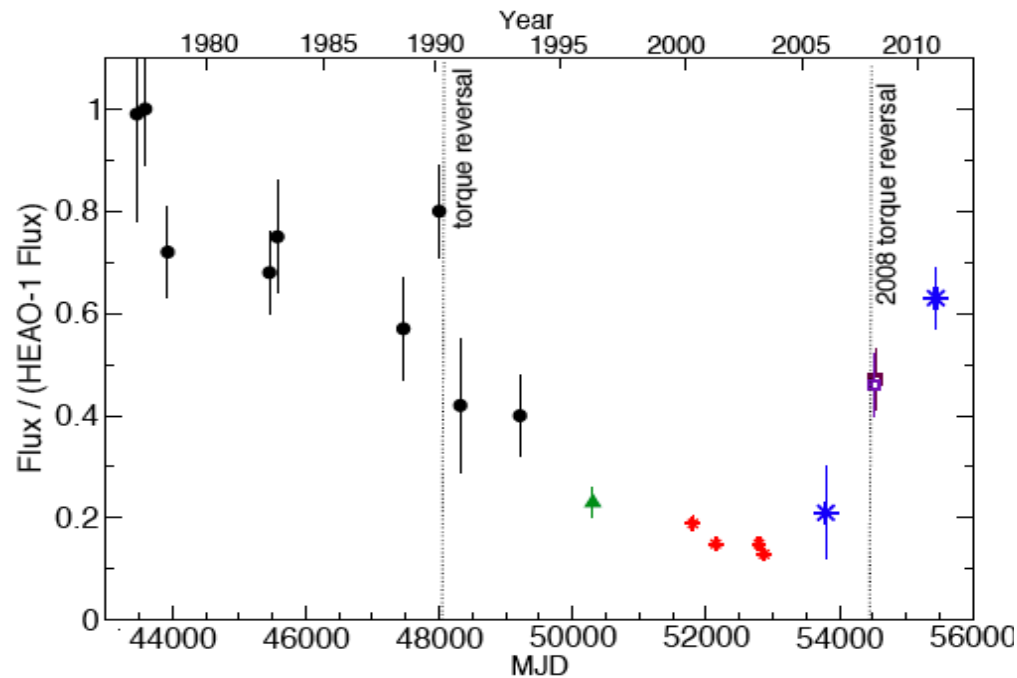


**4U1626-67**

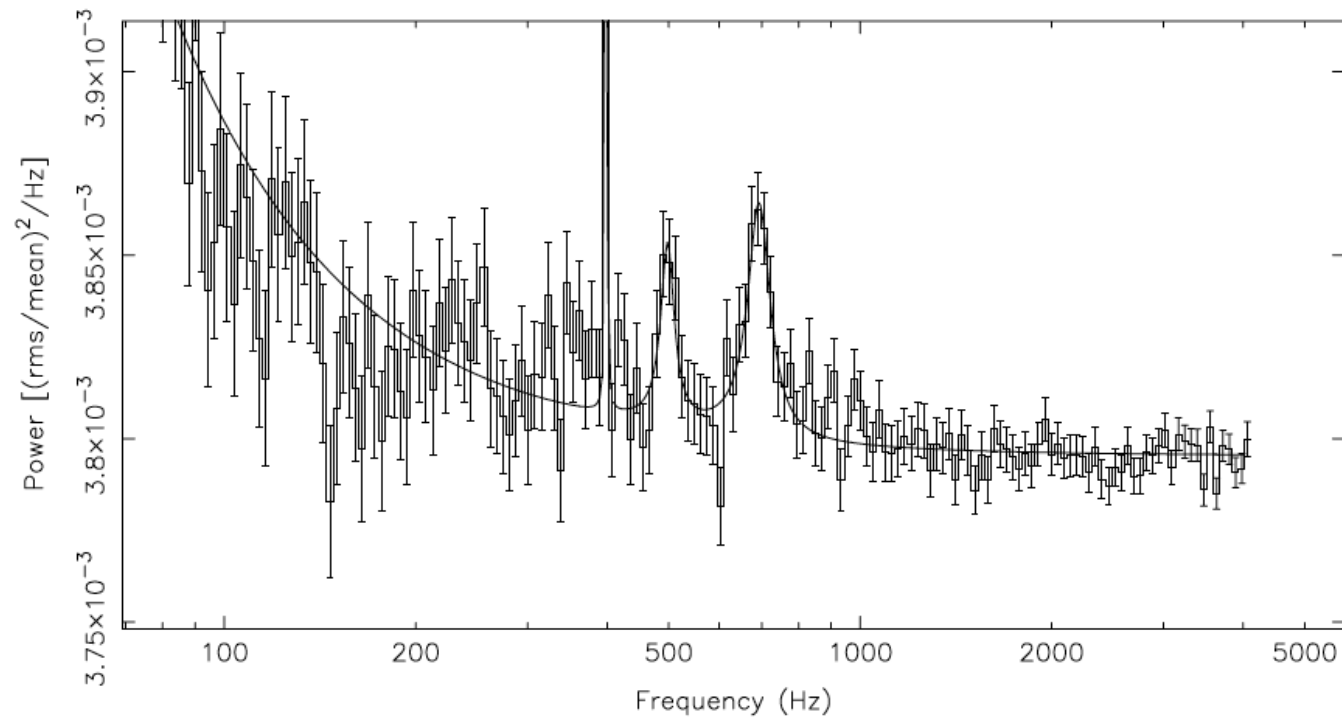
**7.66s**

**Transition lasted 150 days**

*Camero-Arranz et al. 2010,2012*



# kHz QPOs in Accreting Millisecond Pulsars

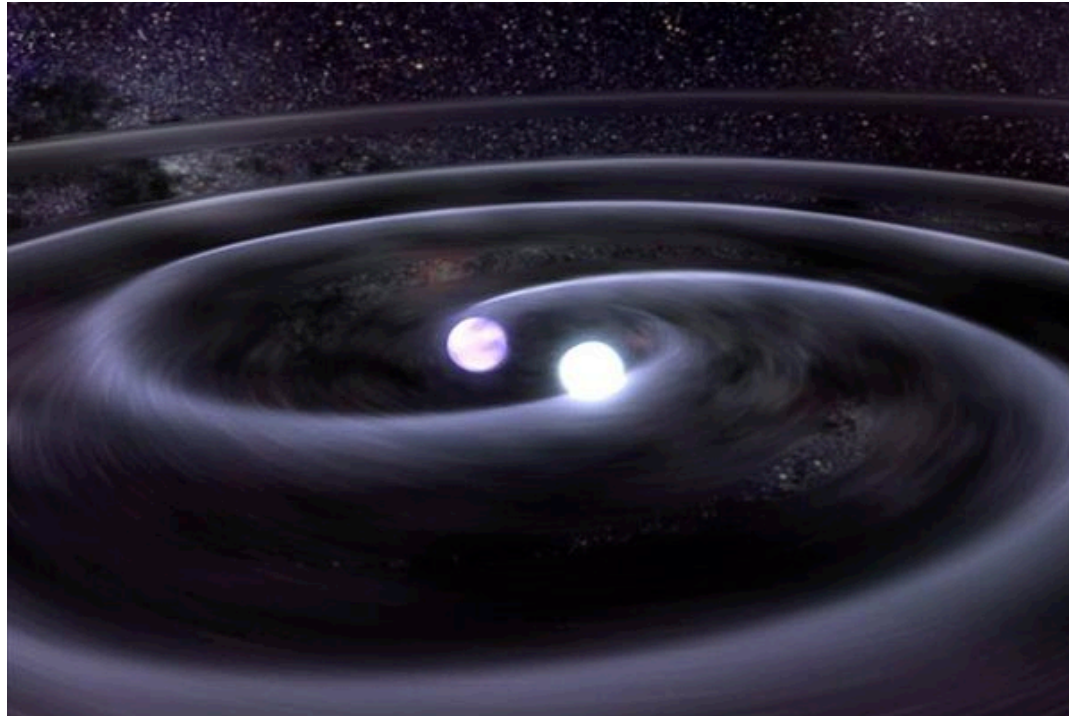


*Van der Klis 2005*

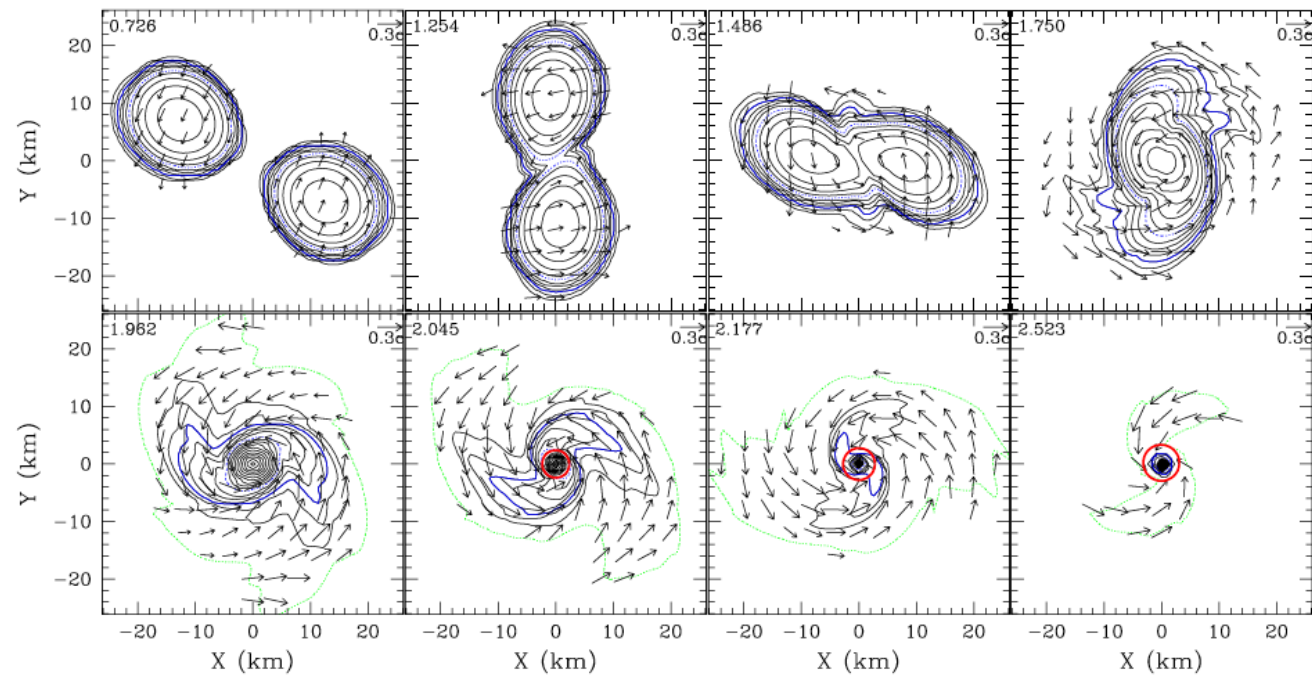
SAX J1808.4-3658:  $\nu_s = 401$  Hz,  $\nu_h - \nu_l \simeq \nu_s/2$  ( $\pm$ a few Hz)

XTE J1807.4-294:  $\nu_s = 191$  Hz,  $\nu_h - \nu_l \simeq \nu_s$

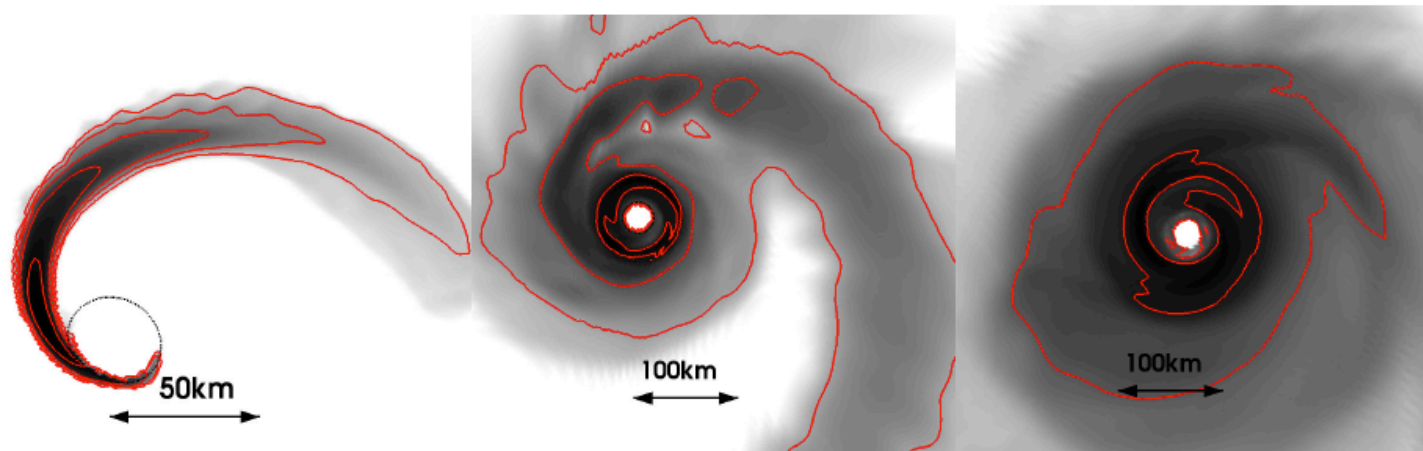
# Merging Neutron Stars



***NS/NS and NS/BH binaries:*** GWs for LIGO/VIRGO  
EM counterparts (short GRBs, kiloNova)



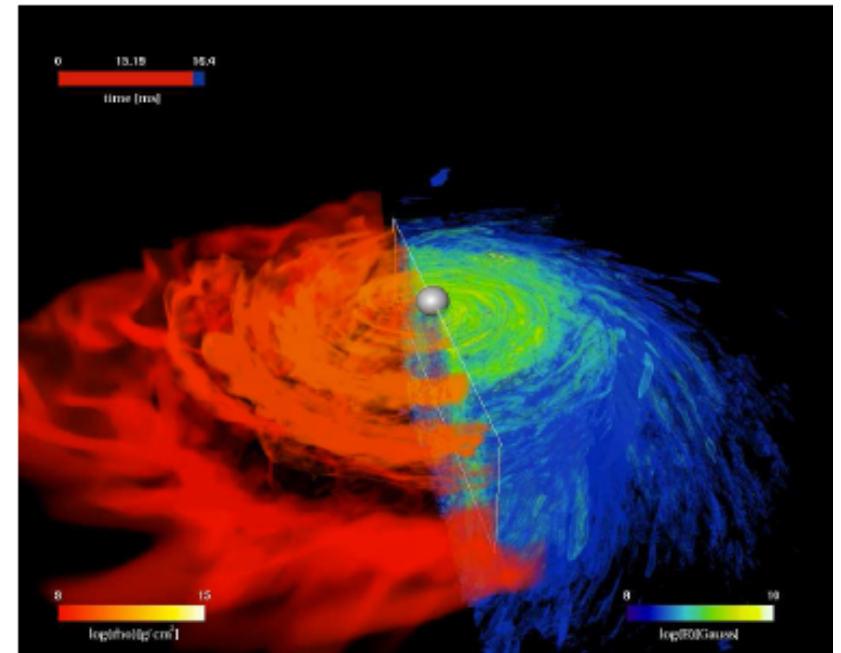
*Shibata et al. 2006*



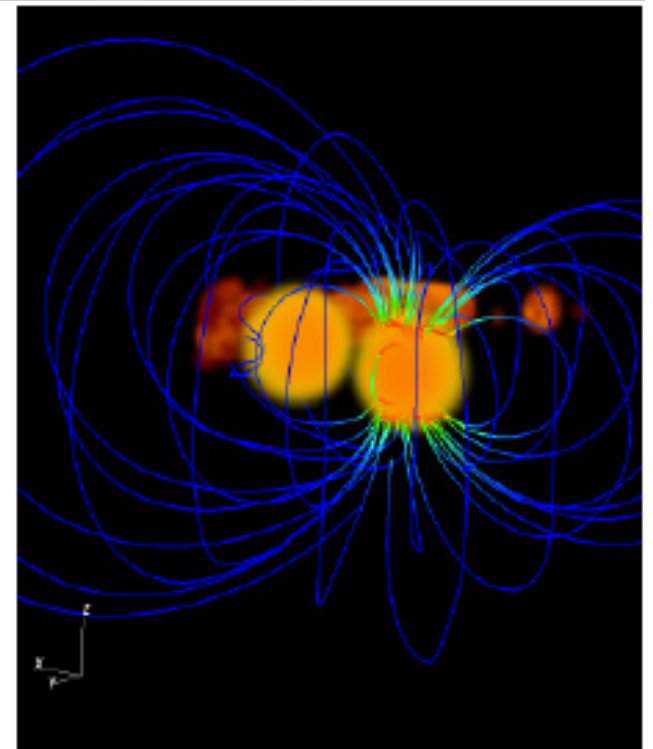
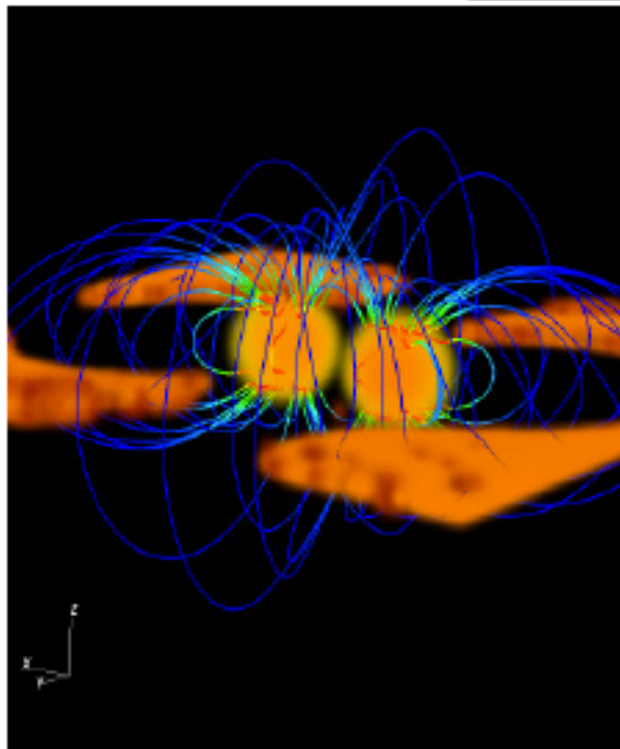
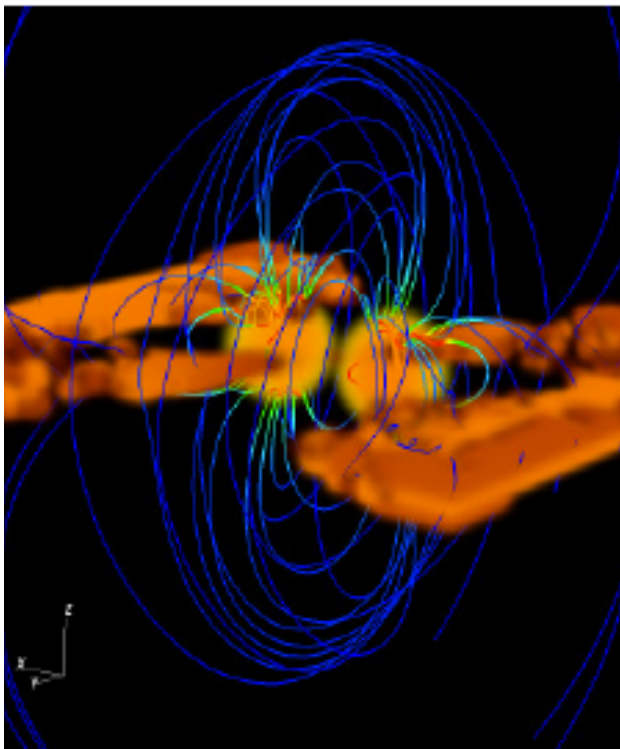
*Foucart et al. (Cornell) 2011,13*

# Merger Simulation with B Fields

*Giacomazzo,  
Rezzolla et al 2011*

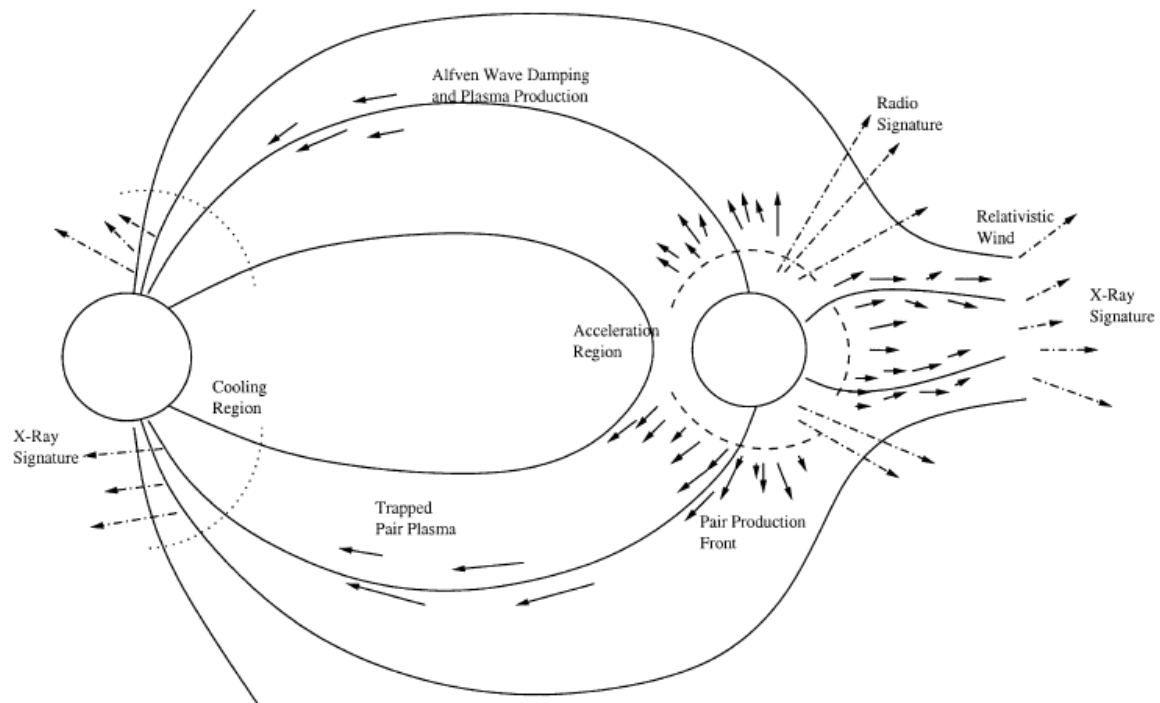


*Palenzuela, Lehner et al. 2013*



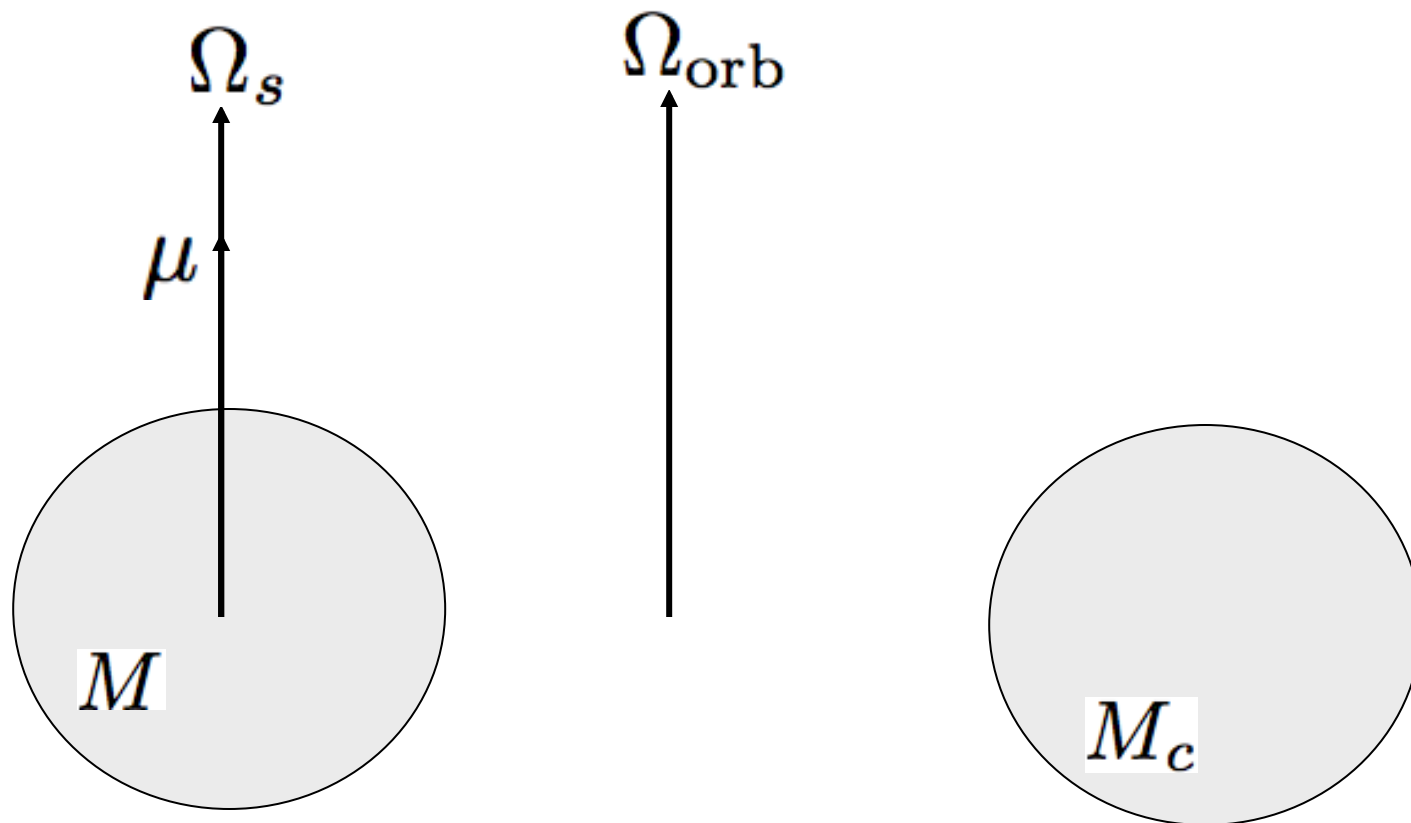


# Merger of Magnetospheres



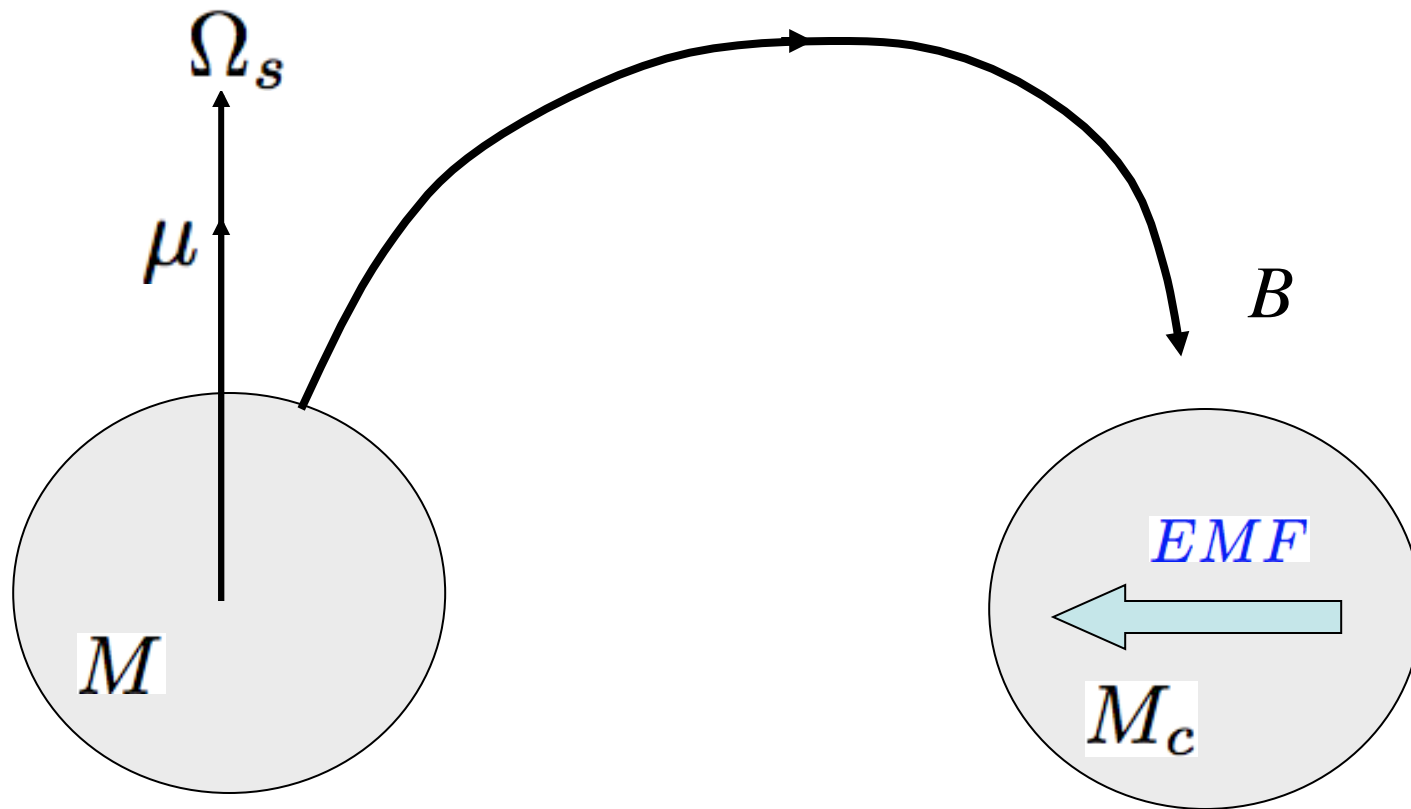
*Hansen & Lyutikov 2001*





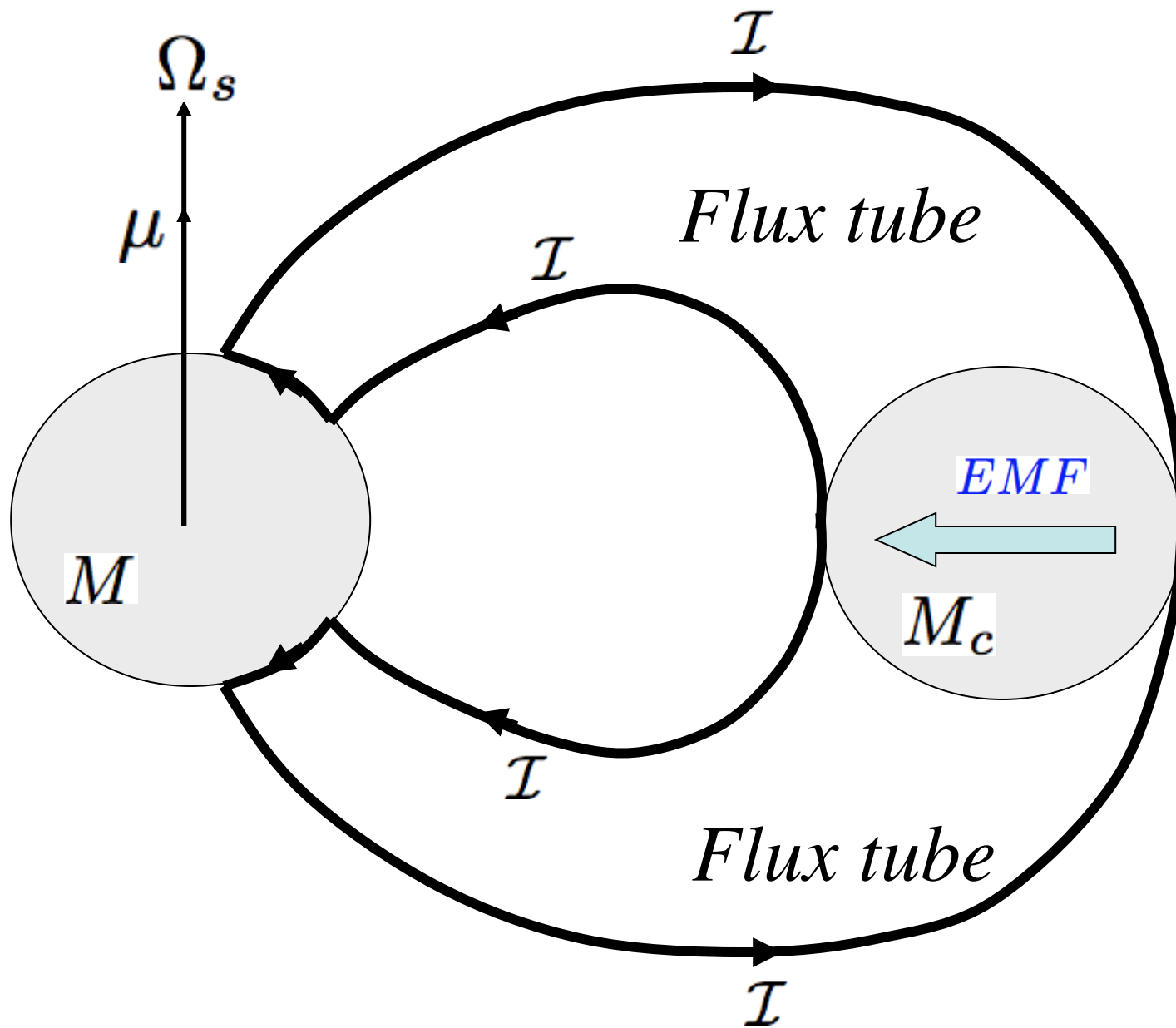
Consider a binary with

- magnetic NS ( $>10^{12}\text{G}$ ) + non-magnetic NS
- embedded in a tenuous plasma (magnetosphere)

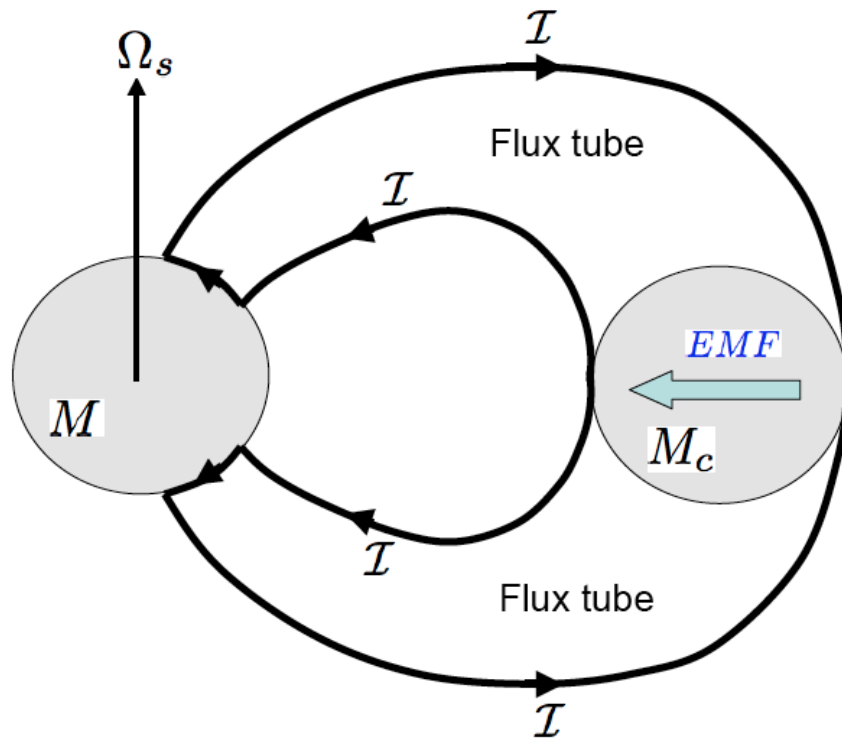


$$EMF : \quad \Phi = 2R_c \left| \frac{\mathbf{v}}{c} \times \mathbf{B} \right|$$

e.g.  $\Phi \sim 10^{13}$  Volt at  $f_{\text{orb}} = 20$  Hz



# DC Circuit Powered by Orbital Motion



$$\text{EMF : } \Phi = \frac{2\mu R_c}{ca^2}(\Omega_{\text{orb}} - \Omega_s)$$

$$\text{Current : } \mathcal{I} = \frac{\Phi}{\mathcal{R}}$$

$$\text{Dissipation : } \dot{E}_{\text{diss}} = \frac{\Phi^2}{\mathcal{R}}$$

# Energy Dissipation in the Magnetosphere of Pre-merging NS Binary

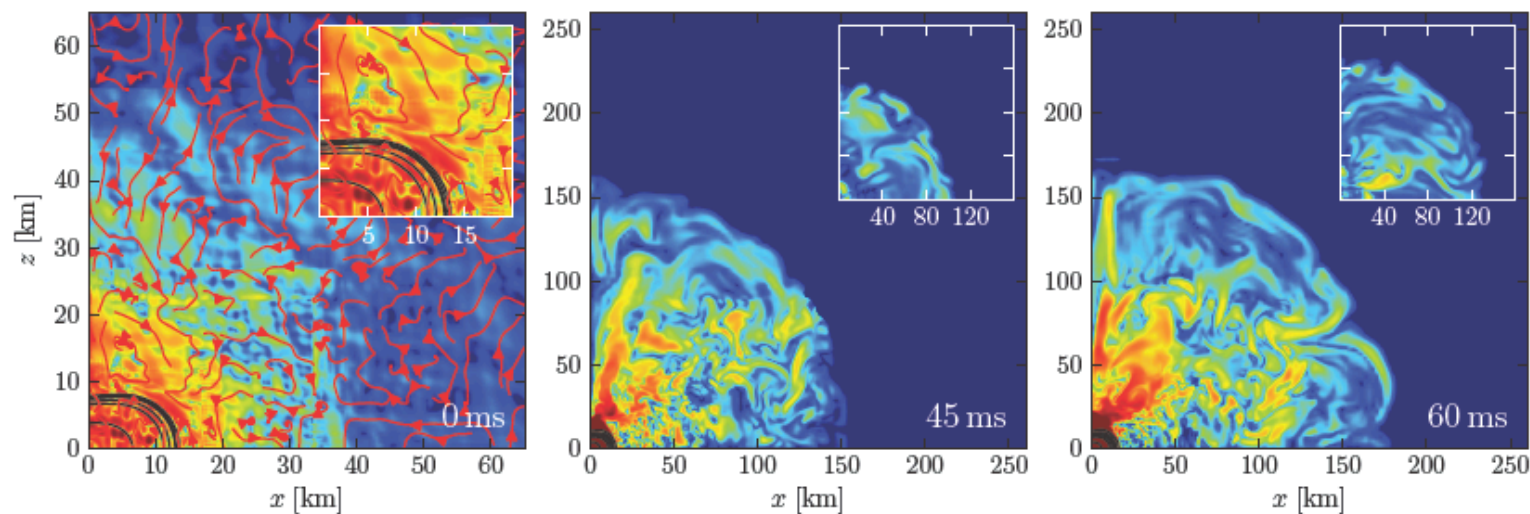
*DL 2012*

$$\dot{E}_{\text{max}} \simeq 7 \times 10^{44} \left( \frac{B_{\text{NS}}}{10^{13} \text{ G}} \right)^2 \left( \frac{a}{30 \text{ km}} \right)^{-13/2} \text{ erg s}^{-1}$$

- This  $\dot{E}$  will not affect orbital decay rate (GW signal)
  - Radio emission prior to binary merger (?) cf. Vietri 96; Hansen & Lyutikov 01
- cf. isolated pulsars:

$$\dot{E} \simeq 10^{33} \left( \frac{B_{\text{NS}}}{10^{13} \text{ G}} \right)^2 \left( \frac{P}{1 \text{ s}} \right)^{-4} \text{ erg s}^{-1}$$

# Magnetic Fields in the Merger Remnant



*Siegel, Cioffi & Rezzolla 2014*

- Field amplification by differential rotation (MRI resolved?)
- Wind/outflow
- Formation of ms magnetar?

# Polarized (Surface) X-Rays from Highly Magnetized Neutron Stars

1. Basic polarization signals
2. QED effects in polarization signals
3. Probe axions

## **Surface emission from magnetic NSs is highly polarized (up to 100%)**

Gnedin & Sunyaev 1974

Pavlov & Shibunov 1978

Meszaros et al. 1988

Pavlov & Zavlin 2000

Ho & DL 2001

Heyl et al. 2003

.....



# Photon Polarization Modes in a Magnetized Plasma

$$(\omega \ll \omega_{ce} = 11.6 B_{12} \text{ keV})$$

## Ordinary Mode (O-mode, // -mode):

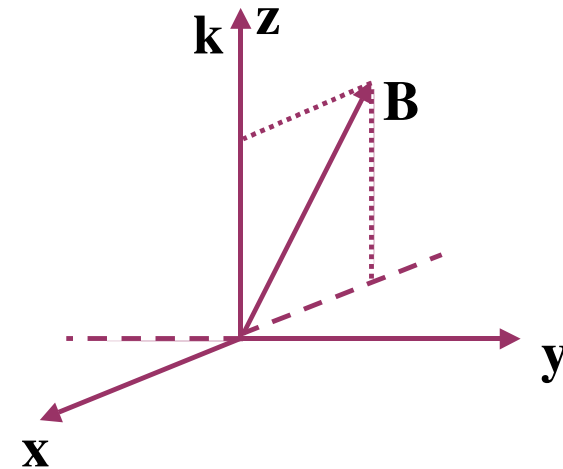
**E** nearly in the **k-B** plane

$$|K| = |E_x/E_y| \gg 1$$

## Extraordinary Mode (X-mode, $\perp$ -mode):

**E** nearly  $\perp$  **k-B** plane

$$|K| = |E_x/E_y| \ll 1$$

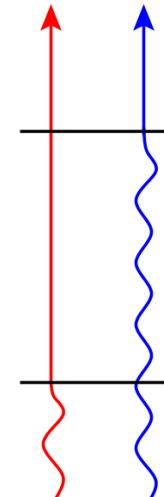


**The two modes have different opacities (scattering, absorption):** X-mode O-mode

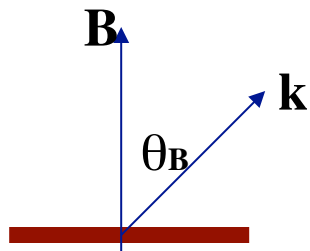
$$K_{\text{(O-mode)}} \sim K_{(B=0)}$$

$$K_{\text{(X-mode)}} \sim K_{(B=0)} (\omega/\omega_{ce})^2$$

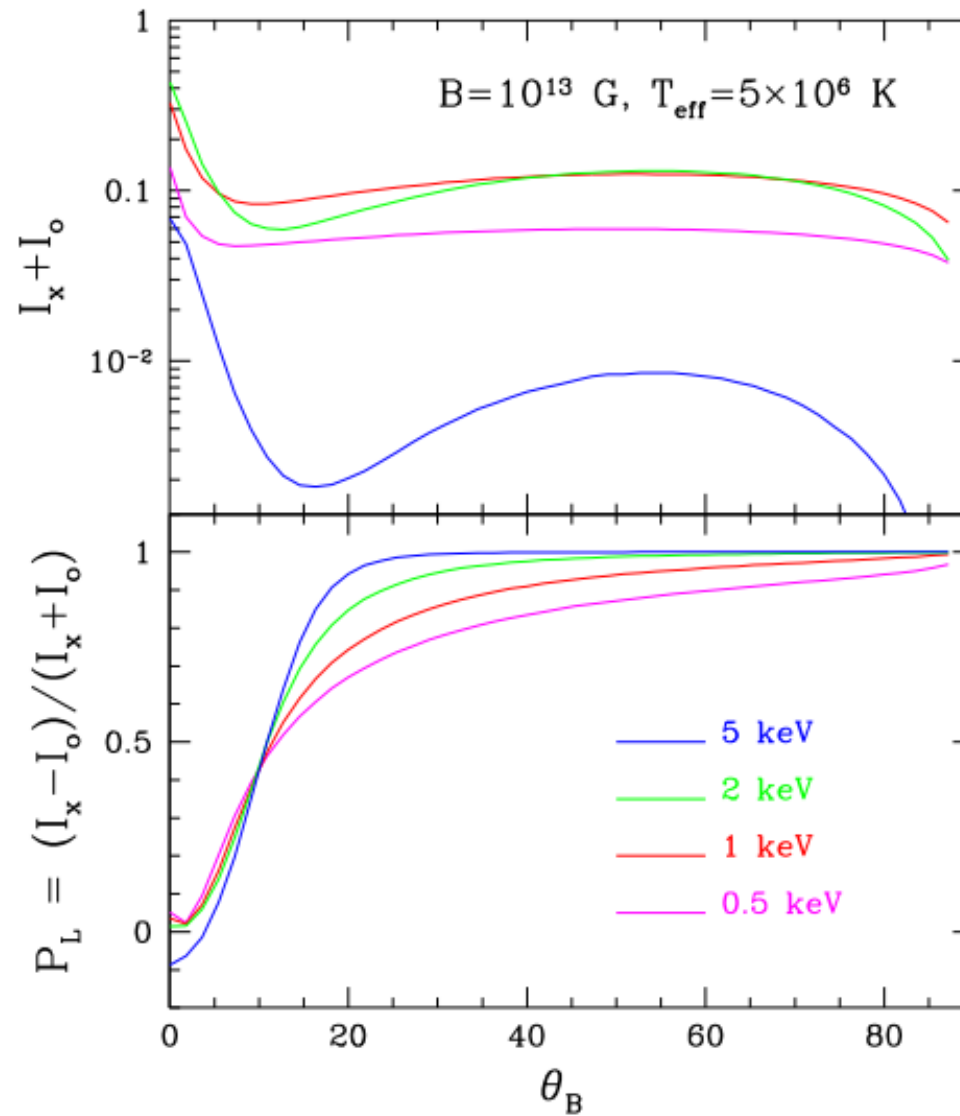
**X-mode photons are the main carrier of X-ray flux**  
(Two photospheres)



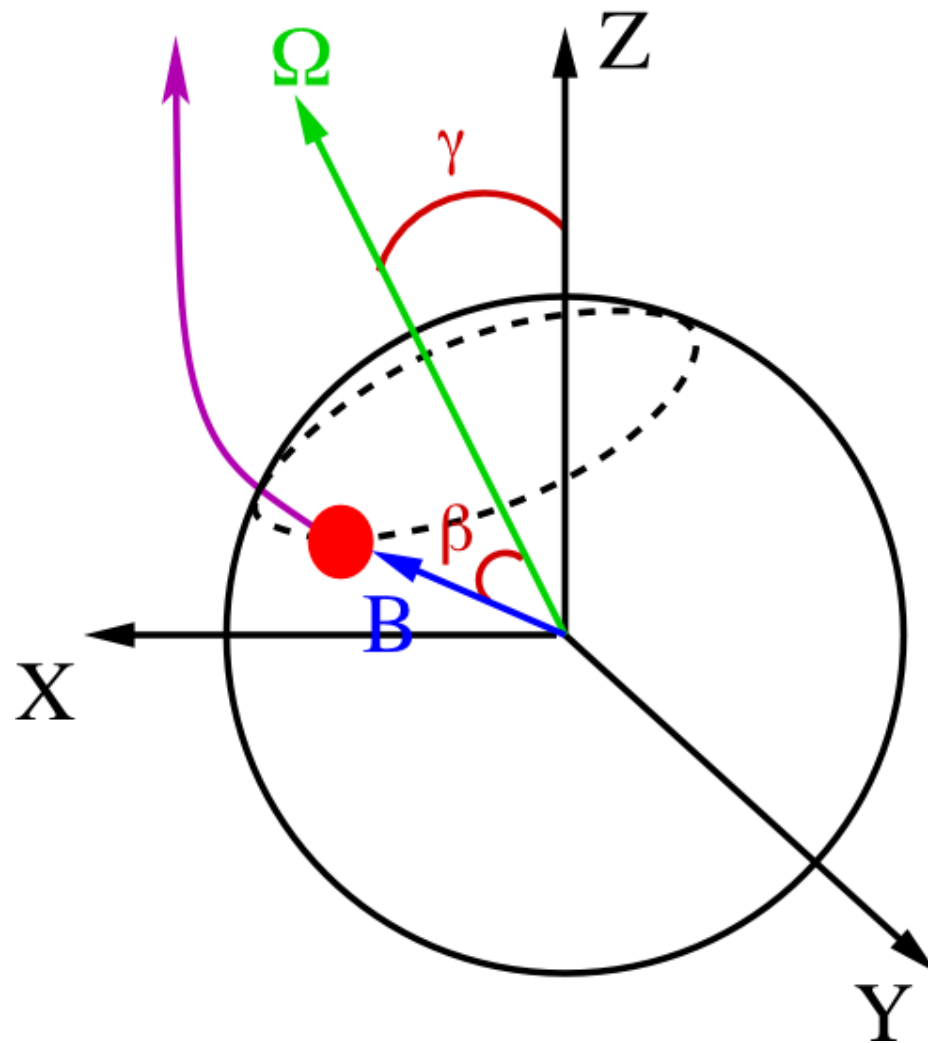
## Putting a polarimeter on the NS surface...



Degree of linear  
Polarization at  
emission point

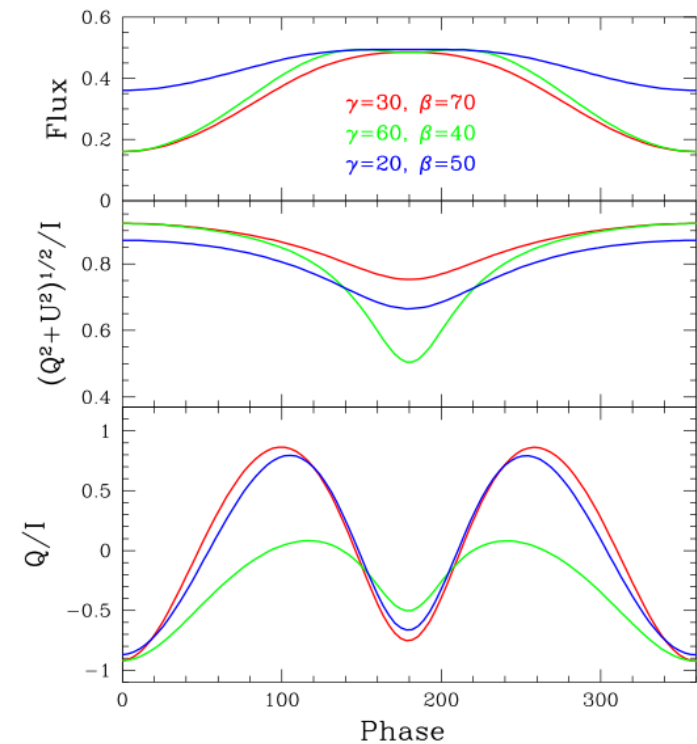


# Observer



# General Expected X-ray Polarization Characteristics

- Polarization vector  $\perp$  or  $\parallel$  to  $\mathbf{k}$ - $\boldsymbol{\mu}$  plane (depending on E and surface  $|\mathbf{B}|$ ) even when surface field is non-dipole!
- Linear polarization sweep  $\Rightarrow$  geometry (“rotating vector model” for radio pulsars)
- Polarization signals can be very different even when total intensities are similar



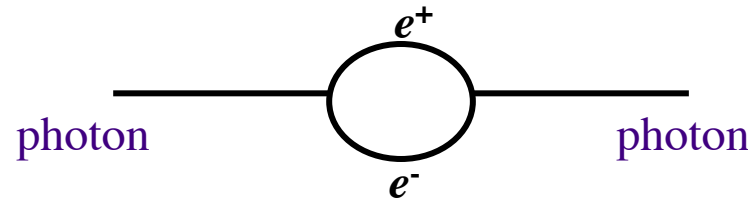
$$\frac{(Q^2 + U^2)^{1/2}}{I} = \text{Linear Polarization Fraction}$$

$$\frac{Q}{(Q^2 + U^2)^{1/2}} = \cos 2\Phi_{\text{Pl}}$$

## Information Carried by Polarization Signals:

- Geometry (dipole field, rotation axis)
- Dependence on surface field strength
- Modest dependence on  $M/R$
- **QED effects**

# QED Effect: Vacuum Polarization in Strong B



Heisenberg & Euler,  
Weisskopf, Schwinger,  
Adler...

Dielectric tensor:  $\epsilon = \mathbf{I} + \Delta\epsilon_{\text{vac}}$

$$|\Delta\epsilon_{\text{vac}}| \sim 10^{-4}(B/B_Q)^2, \text{ with } B_Q = 4.4 \times 10^{13} \text{ G}$$

Two photon modes in magnetized vacuum:

Ordinary mode ( $//$ )

Extraordinary mode ( $\perp$ )

**Influence polarization signals in two ways:**

1. In NS atmosphere: mode conversion

2. Polarization evolution in magnetosphere: mode decoupling

# QED Effect in NS Atmosphere

Dielectric tensor of magnetized plasma including vacuum polarization

$$\boldsymbol{\epsilon} = \mathbf{I} + \Delta\boldsymbol{\epsilon}^{(\text{plasma})} + \Delta\boldsymbol{\epsilon}^{(\text{vac})}$$

where  $\Delta\boldsymbol{\epsilon}^{(\text{vac})} \sim 10^{-4} (B/B_Q)^2 f(B)$ , with  $B_Q = 4.4 \times 10^{13} \text{G}$ ,  $f(B) \sim 1$

cf. Gnedin, Pavlov & Shibano 1978;  
Meszaros & Ventura 1978, etc

## Vacuum resonance:

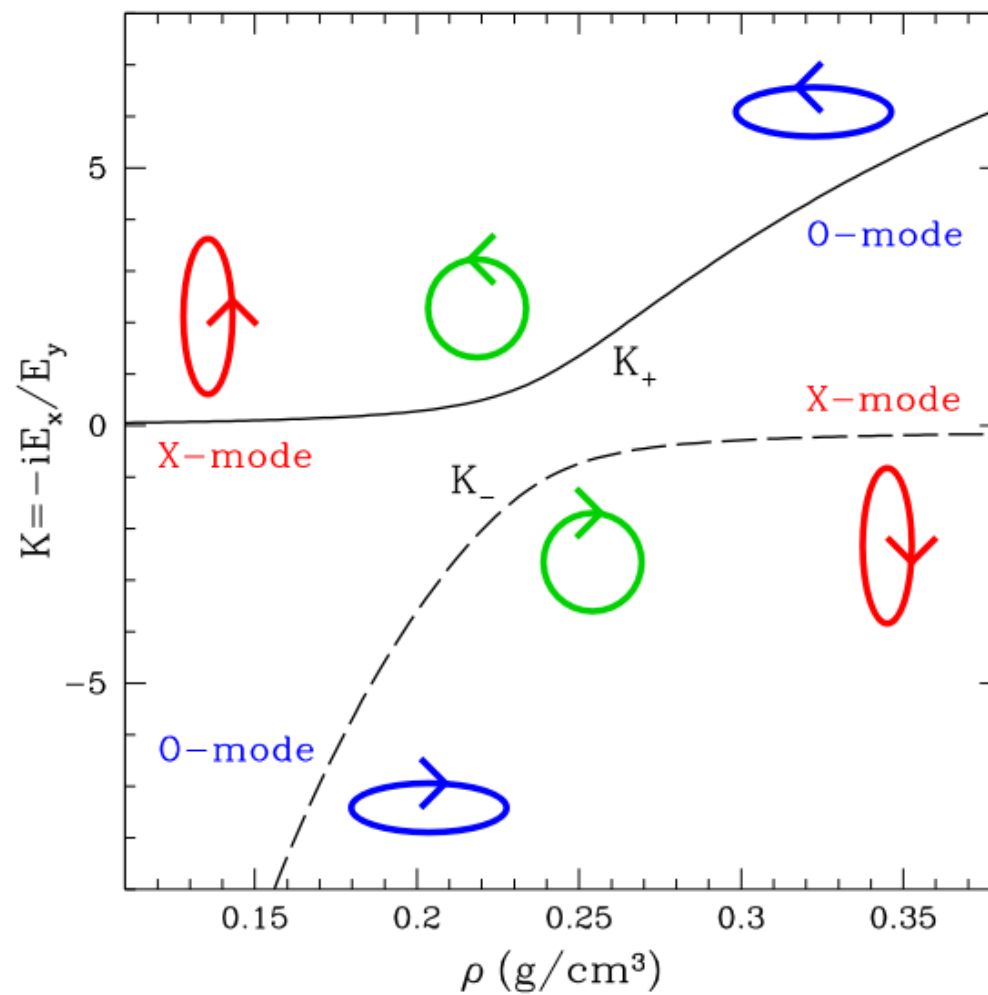
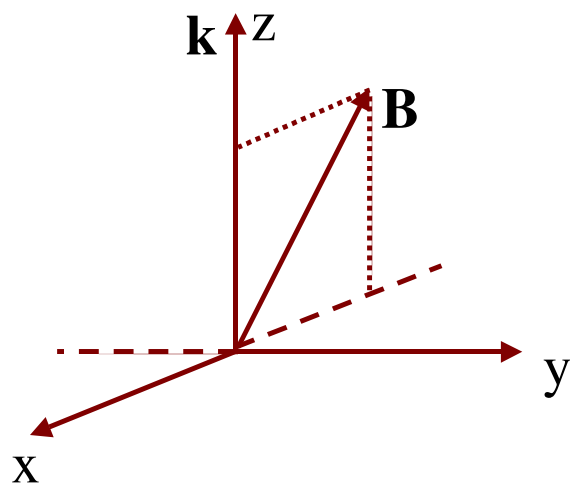
$$\Delta\boldsymbol{\epsilon}^{(\text{plasma})} + \Delta\boldsymbol{\epsilon}^{(\text{vac})} \sim 0$$

depends on  $-(\omega_p/\omega)^2 \propto \rho/E^2$

$$\Rightarrow \rho_{\text{vac}} = 1.0 B_{14}^2 f(B)^{-1} (E/1 \text{ keV})^2 \text{ g cm}^{-3}$$

At resonance, X-mode and O-mode are “similar”

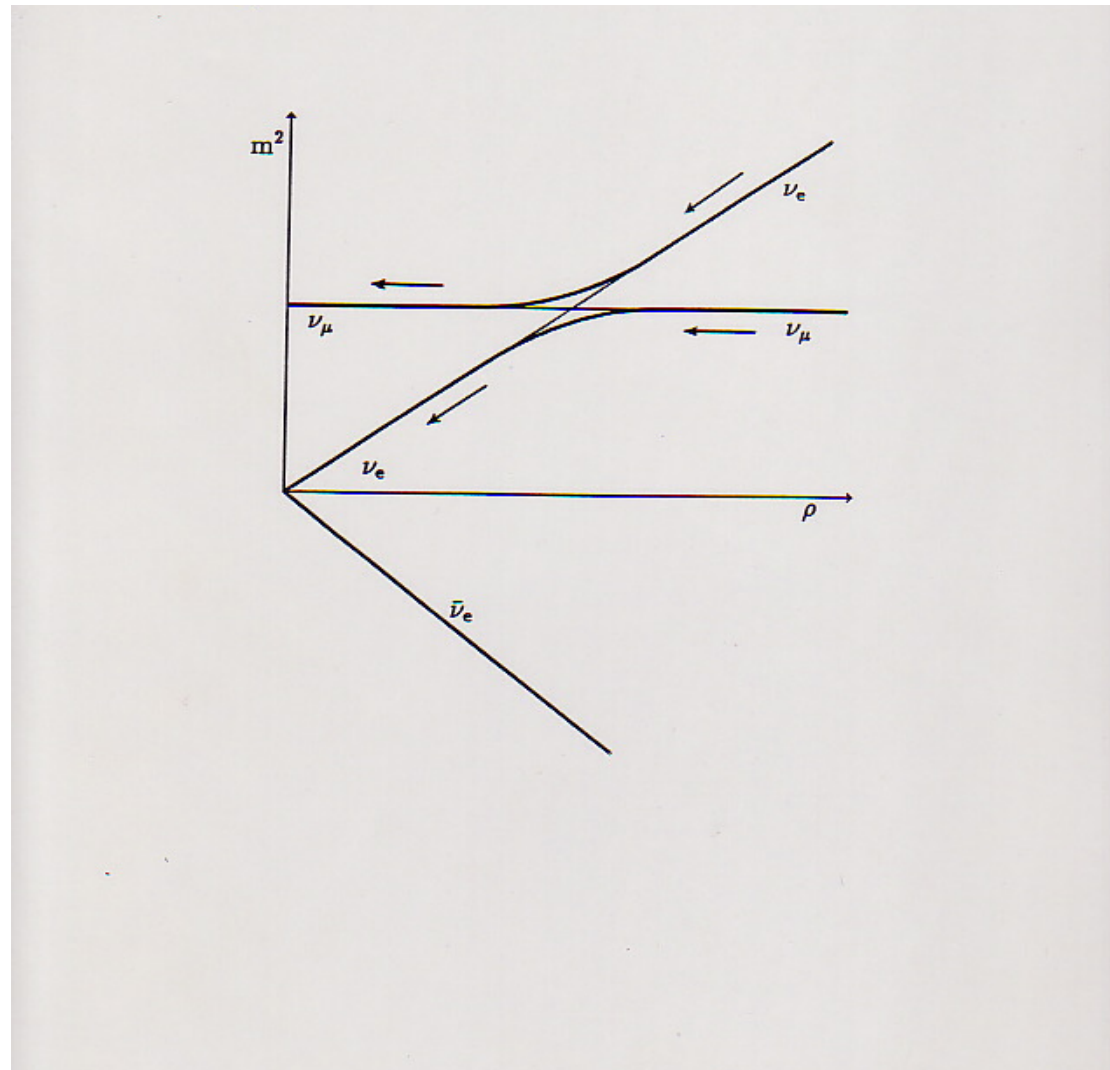
# Polarization of photon modes



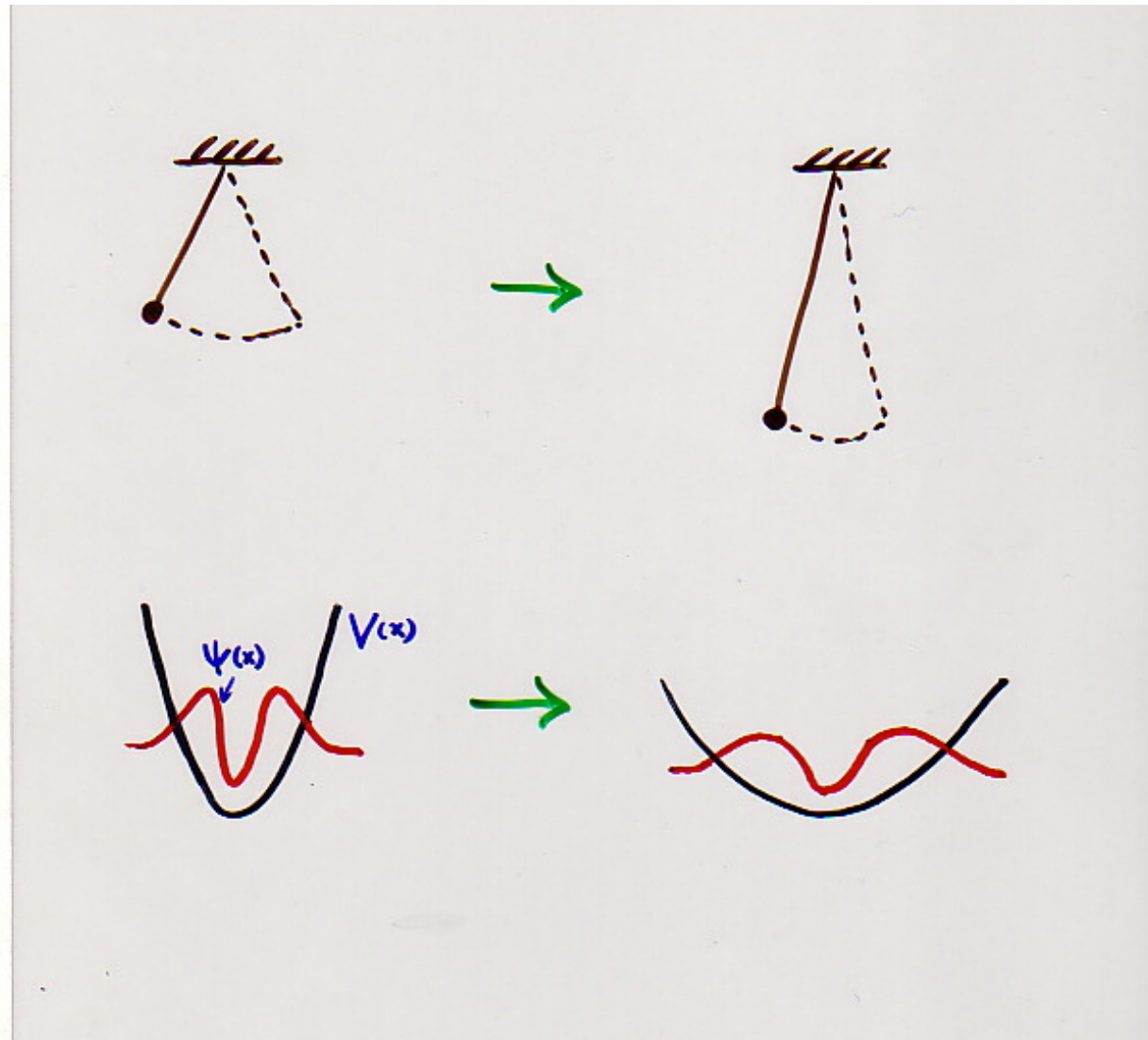
$$B=10^{13} \text{ G}, E=5 \text{ keV}, \theta_B=45^\circ$$



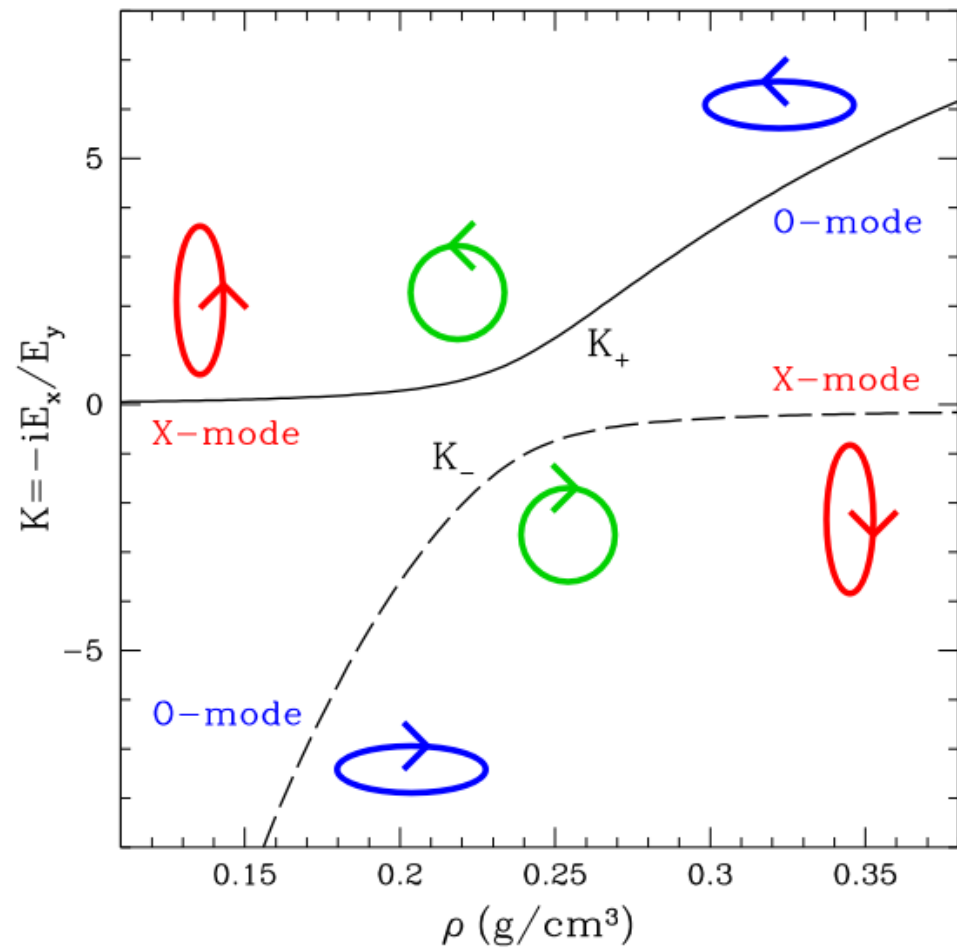
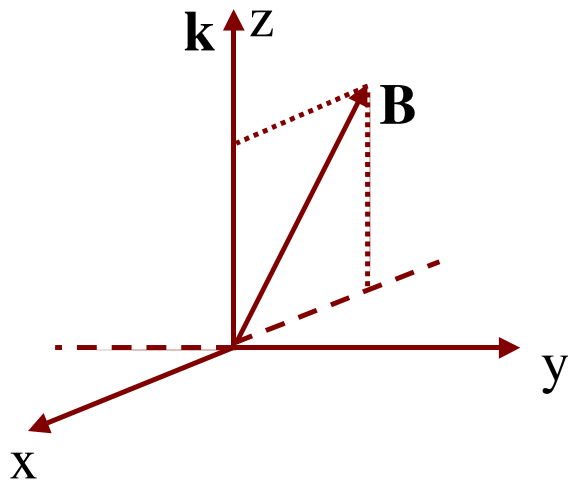
# Mikheyev-Smirnov-Wolfenstein (MSW) Neutrino Oscillation



# Adiabatic Evolution of a Quantum State



“Plasma+Vacuum”  $\Rightarrow$  Vacuum resonance

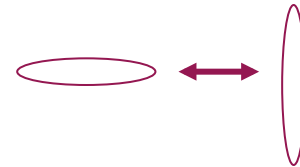


## Adiabatic Condition:

$$\left| n_1 - n_2 \right| \gtrsim ( \cdots ) \left| d\rho/dr \right|$$

→  $E \gtrsim E_{\text{ad}} = 2.5 ( \tan \theta_B )^{2/3} (1 \text{ cm/H})^{1/3} \text{ keV}$

Photons with  $E > 2 \text{ keV}$ , mode conversion



Photons with  $E < 2 \text{ keV}$ , no mode conversion

In general, nonadiabatic “jump” probability

$$P_{\text{jump}} = \exp [ - (\pi/2) (E / E_{\text{ad}})^3 ]$$

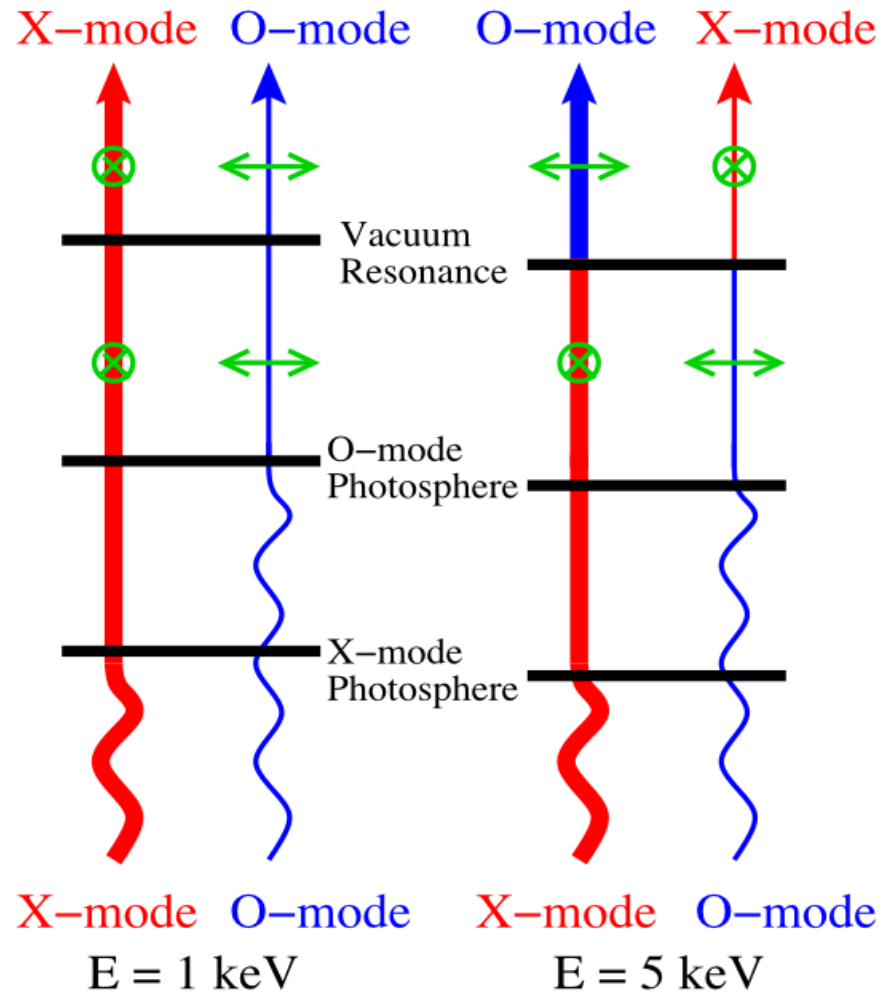
## Recall

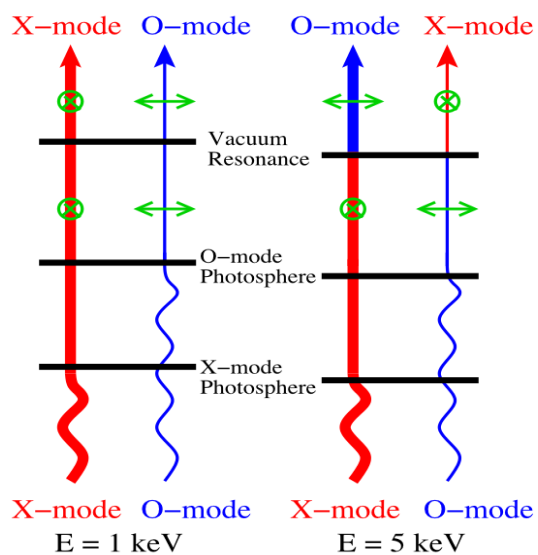
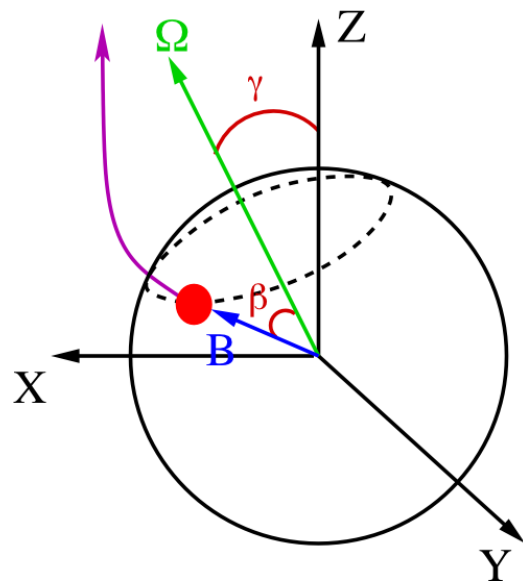
-- X-mode and O-mode have different photospheres

$$\text{-- } \rho_{\text{vac}} = 1.0 B_{14}^2 f(B)^{-1} (E/1 \text{ keV})^2 \text{ g cm}^{-3}$$

For  $B < 7 \times 10^{13} T_6^{-1/8} E_1^{-1/4} \text{ G}$ :

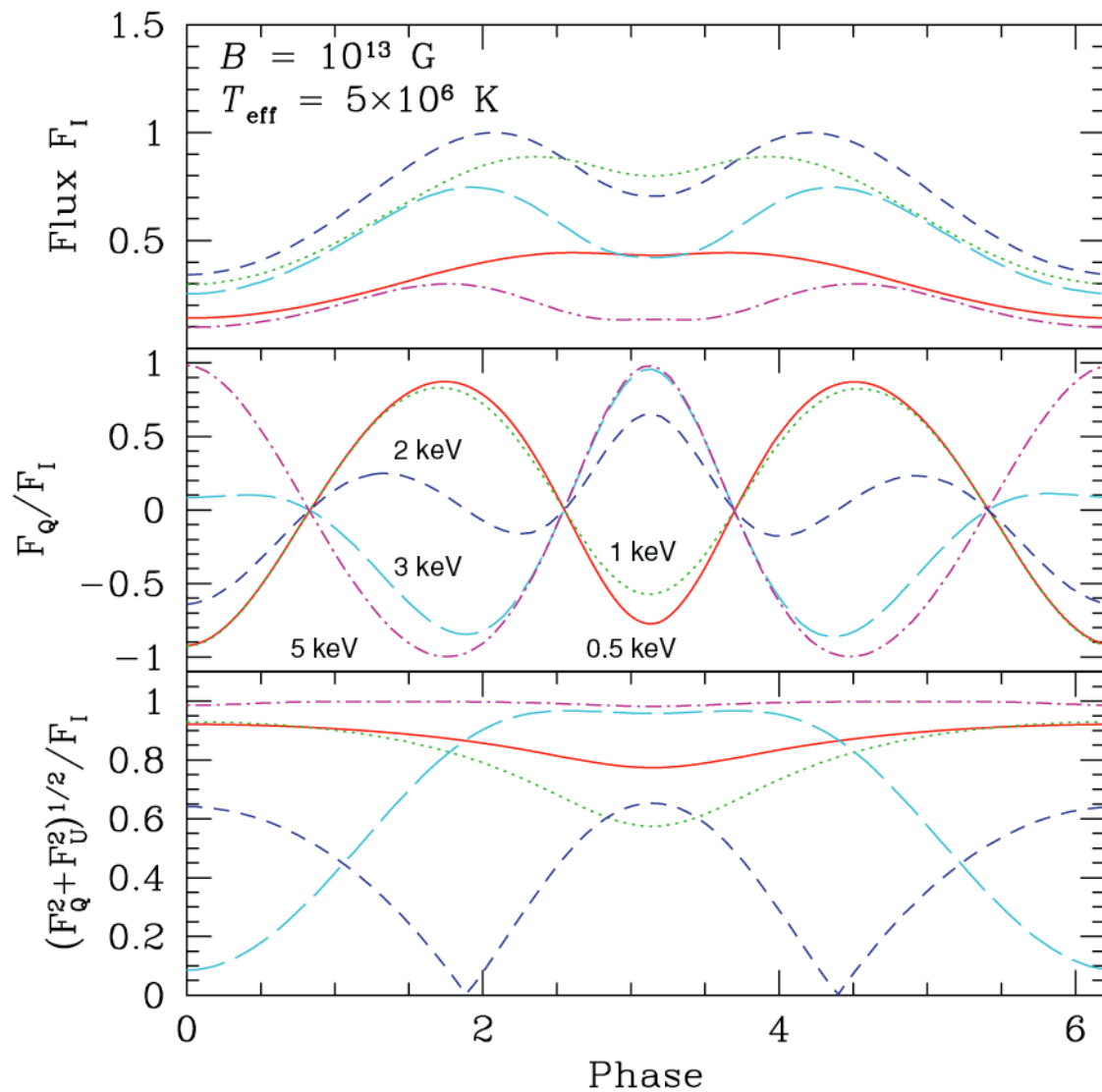
Vacuum resonance lies outside both photospheres





**$B=10^{13}\text{G}$**

$\gamma = 30^\circ, \beta = 70^\circ$

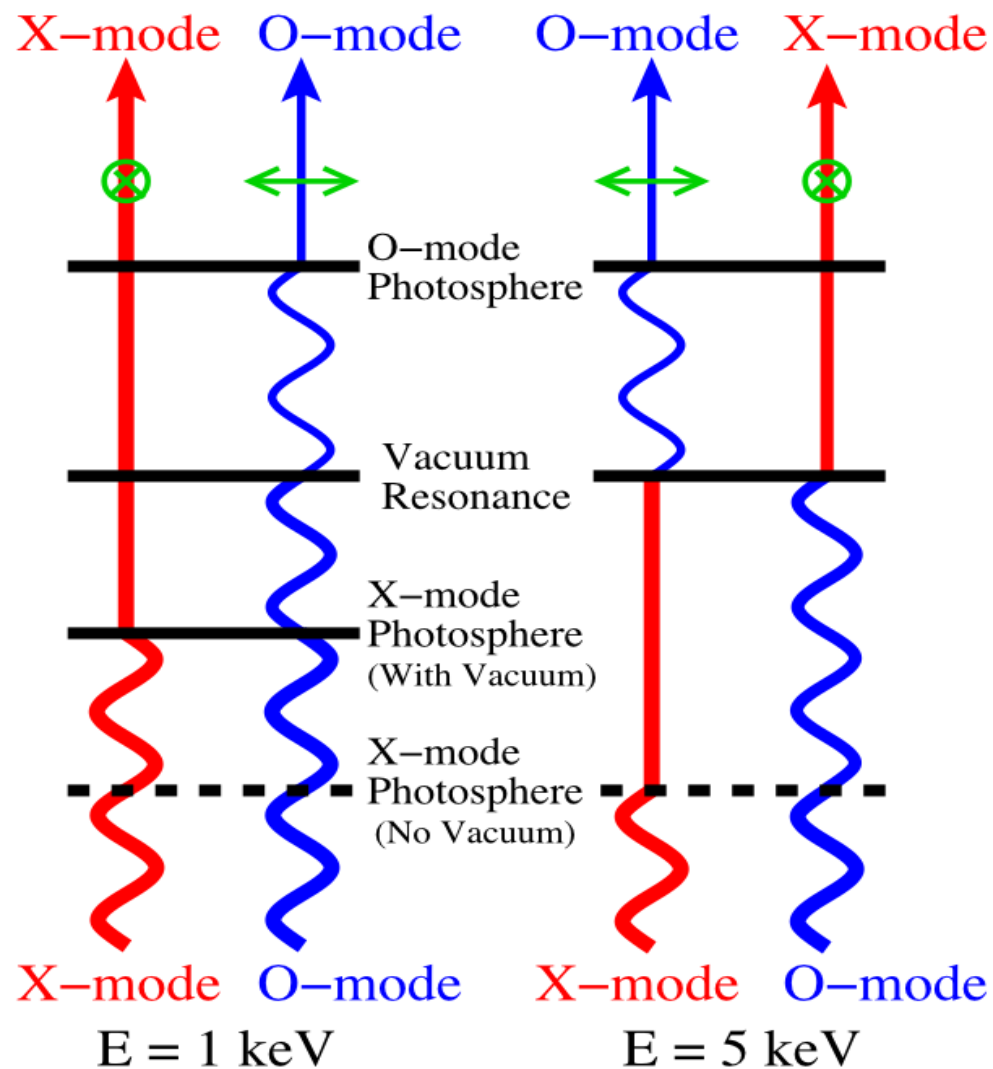


Van Adelsberg & DL 2006 (also DL & Ho 2003)

➡ Plane of linear polarization at  $<1\text{ keV}$  is perpendicular to that at  $>4\text{ keV}$ .

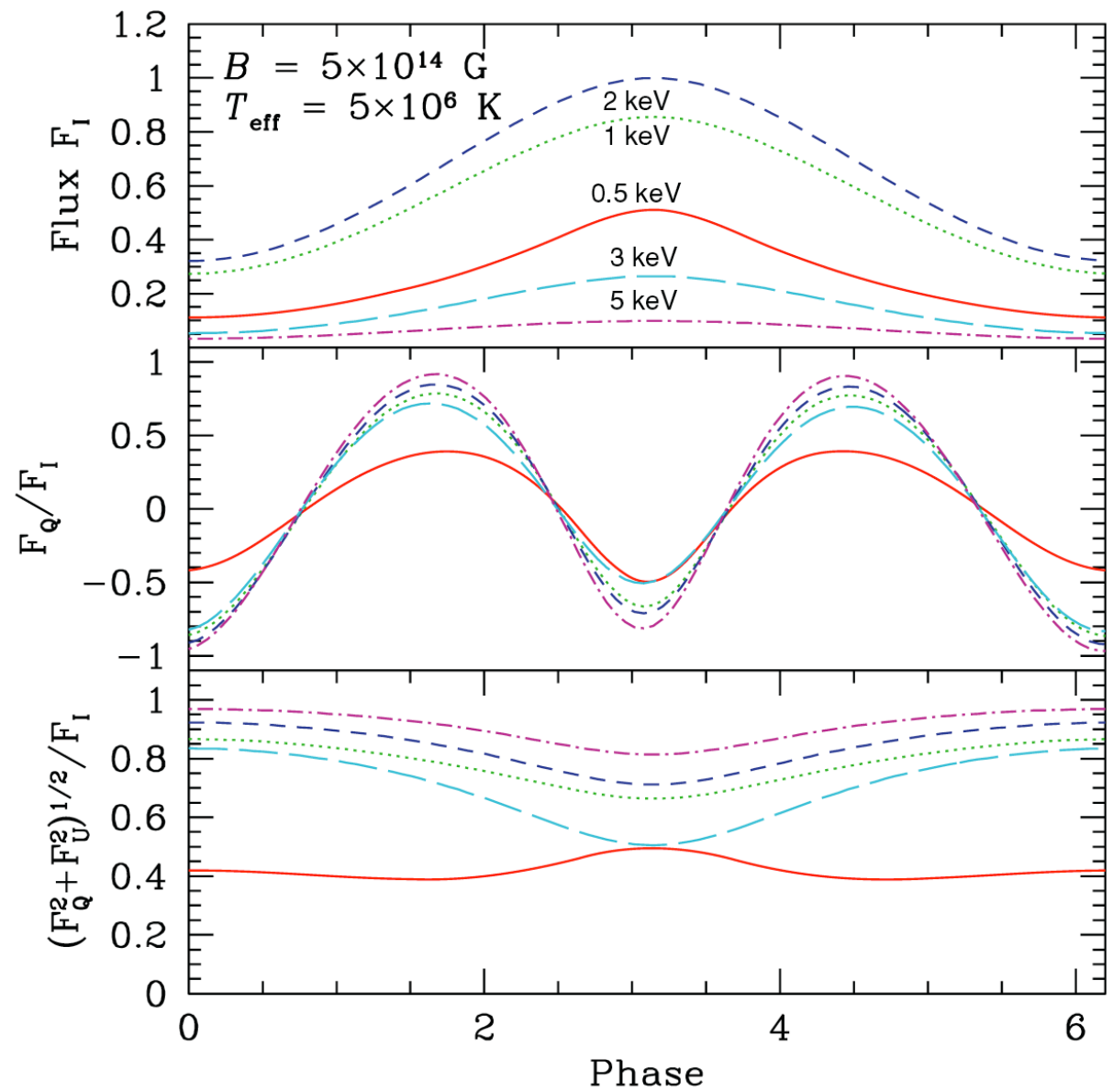
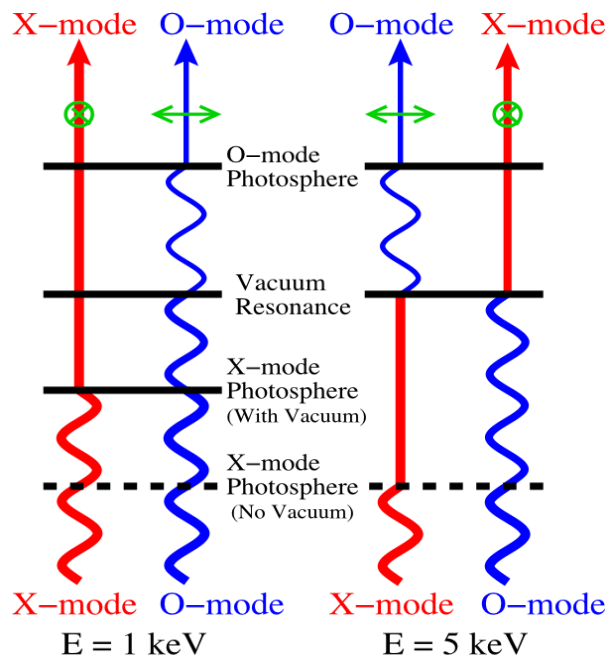
For  $B > 7 \times 10^{13} T_6^{-1/8} E_1^{-1/4} \text{ G}$ :

Vacuum resonance lies between the two photospheres





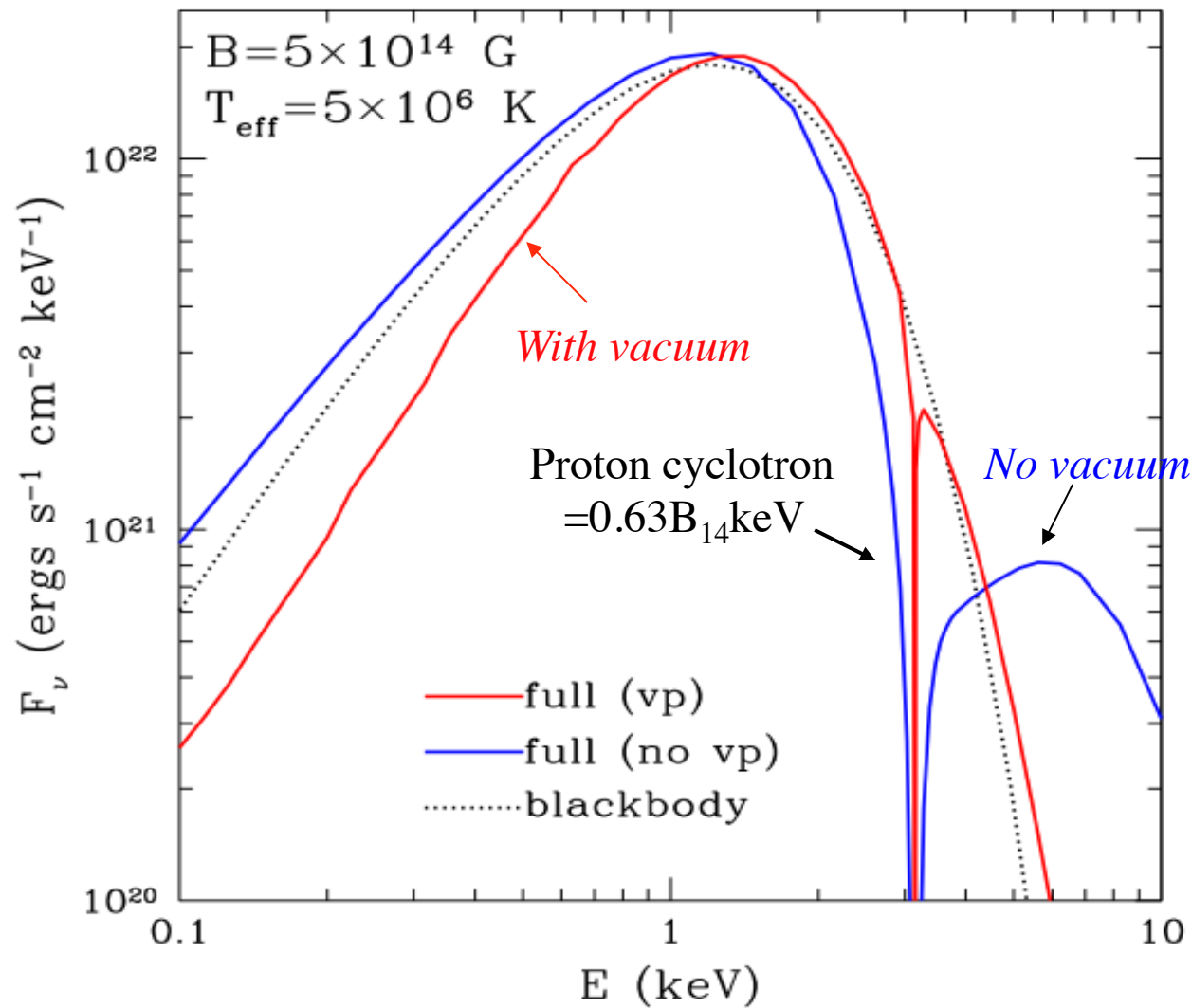
## $B=5 \times 10^{14} \text{ G}$ Model



Plane of linear polarization at different E coincide.

For  $B > 7 \times 10^{13} T_6^{-1/8} E_1^{-1/4} \text{ G}$ :

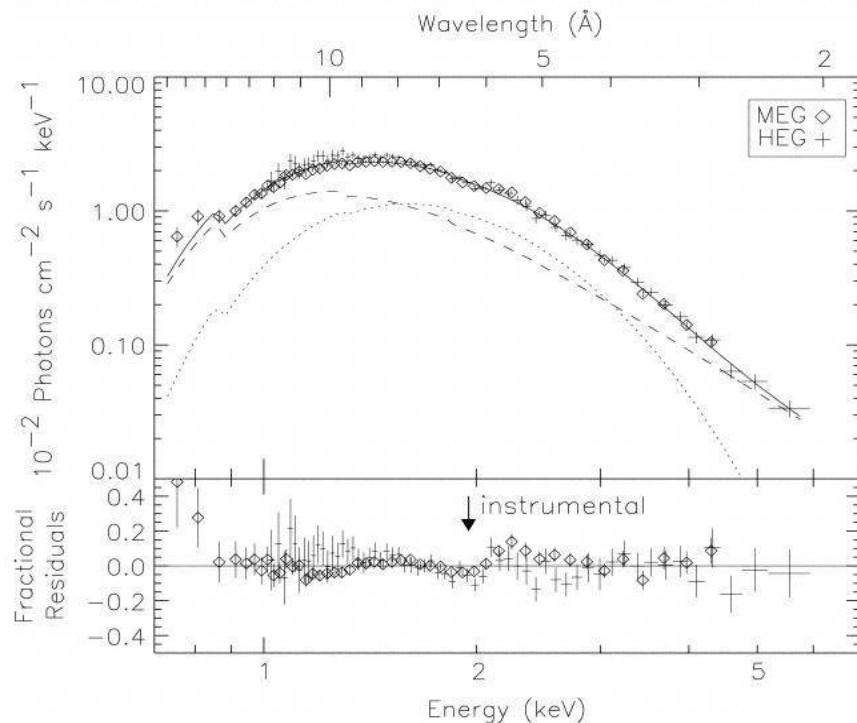
Spectrum is significantly affected by vacuum polarization effect



# Two Examples of AXP Spectra

***AXP 4U0142+61*** (Chandra-HETGS)

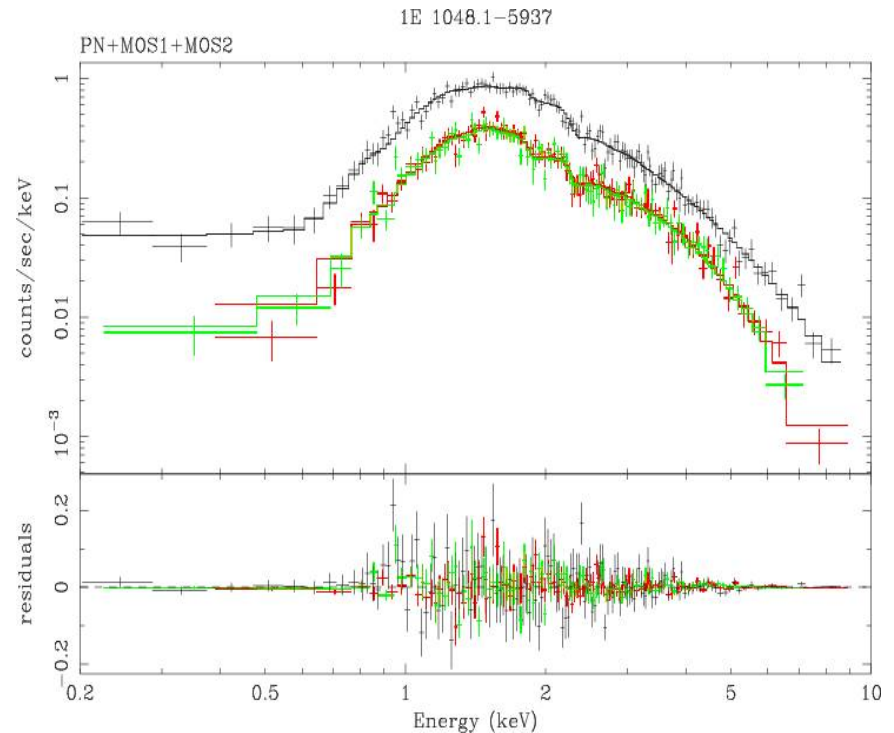
**BB T=0.4 keV, power-law n=3**



Juett et al. 2002; Patel et al 2003

***AXP 1E1048-5937*** (XMM-Newton)

**BB T=0.6 keV, Power-law n=2.9**

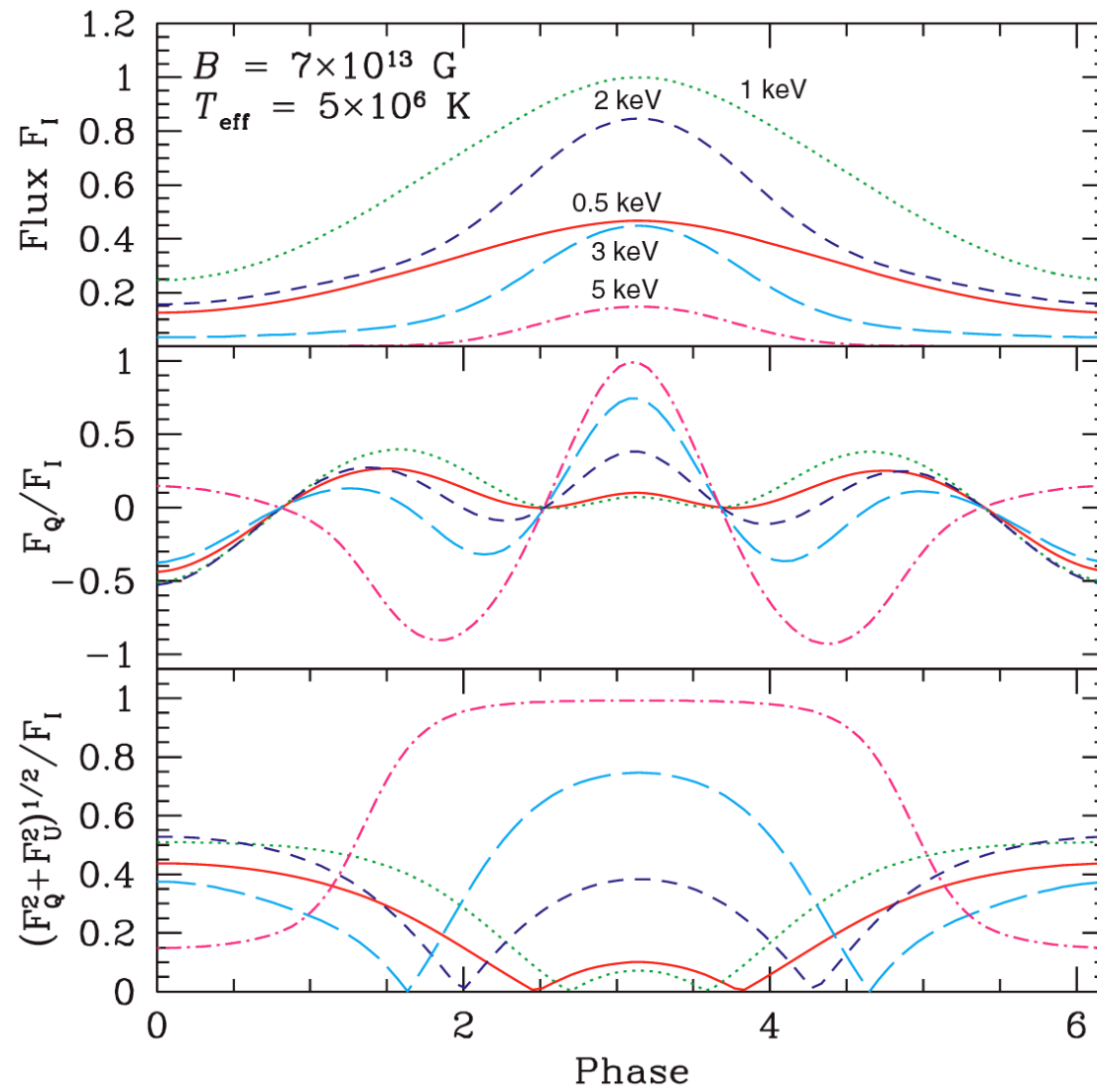


Tiengo et al. 2002

**Ion cyclotron absorption  $E_{\text{Bi}}=0.63 B_{14}$  keV**  
**Why not see?**

**QED at work**

## $B=7 \times 10^{13} \text{ G}$ Model



Van Adelsberg & DL 2006

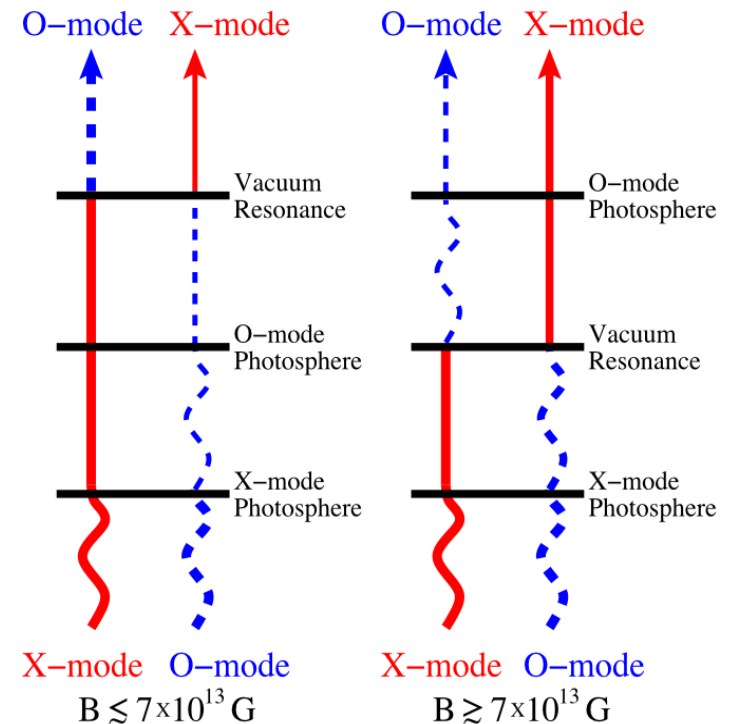
# Recapitulation: Effect of Vacuum Resonance on Surface Emission

**For  $B < 7 \times 10^{13} \text{ G}$**  ( $\rho_{\text{vac}} < \rho_{\text{o-mode}} < \rho_{\text{x-mode}}$ )

- Negligible effect on spectrum  
(spectral line possible: already observed?)
- Dramatic effect on X-ray polarization signals  
(plane of linear polarization depends E)  
--- A “clean” QED signature

**For  $B > 7 \times 10^{13} \text{ G}$**  ( $\rho_{\text{o-mode}} < \rho_{\text{vac}} < \rho_{\text{x-mode}}$ )

- Dramatic effect on spectrum  
(suppress absorption lines, soften hard tails: observations of magnetars)
- Polarization signals affected by QED:  
plane of linear polarization coincides for different E



# **QED Effect in Magnetospheres (=Magnetized Vacuum)**

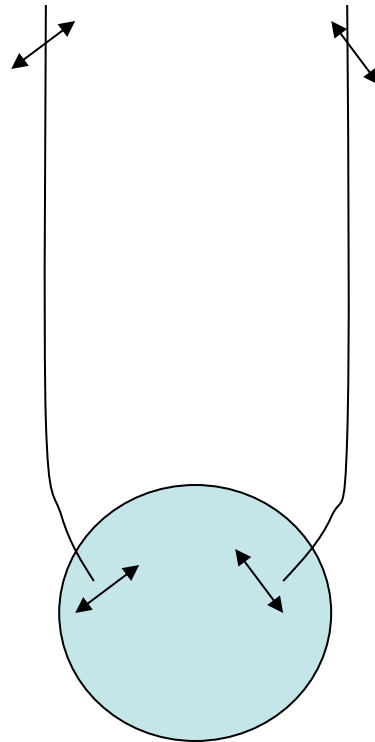
## **Propagation of Polarized Radiation**

# Propagation of Polarization from NS Surface to Observer

What if emission is from large patch of star? Complex surface field?

**Recall:** At the surface, the emergent radiation is dominated by one of the two modes (let's say X-mode, polarized  $\perp$  the local  $\mathbf{B}$ ).

If polarization were parallel-transported to infinity, the net polarization (summed over observable surface of the star) would be reduced.

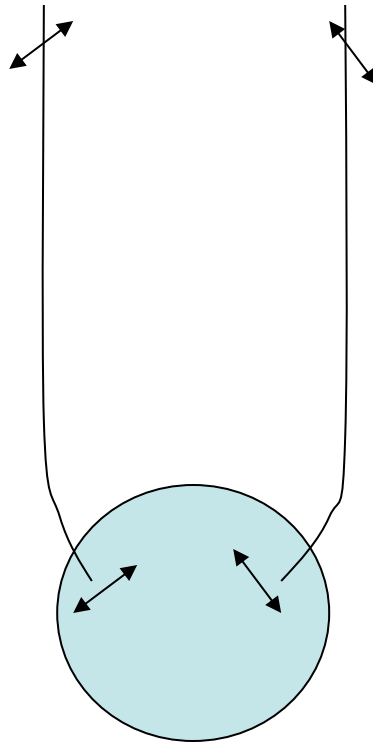


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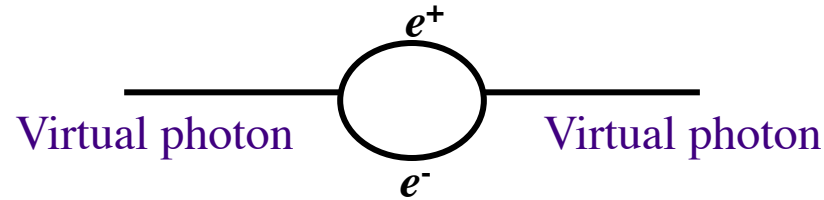


**This is incorrect!**

(Heyl & Shaviv 2002;  
Lai & Ho 2003...)



# Vacuum Polarization in Strong B



Dielectric tensor outside the neutron star:  $\boldsymbol{\epsilon} = \mathbf{I} + \Delta\boldsymbol{\epsilon}^{(\text{vac})}$

where  $\Delta\boldsymbol{\epsilon}^{(\text{vac})} \sim 10^{-4} (B/B_Q)^2 f(B)$ , with  $B_Q = 4.4 \times 10^{13} \text{G}$ ,  $f(B) \sim 1$

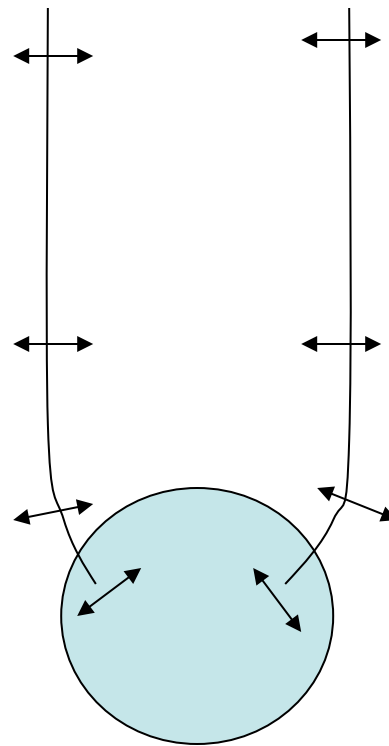
Two photon modes in magnetized vacuum:

Ordinary mode ( $//$ )

Extraordinary mode ( $\perp$ )

$$n_1 \neq n_2$$

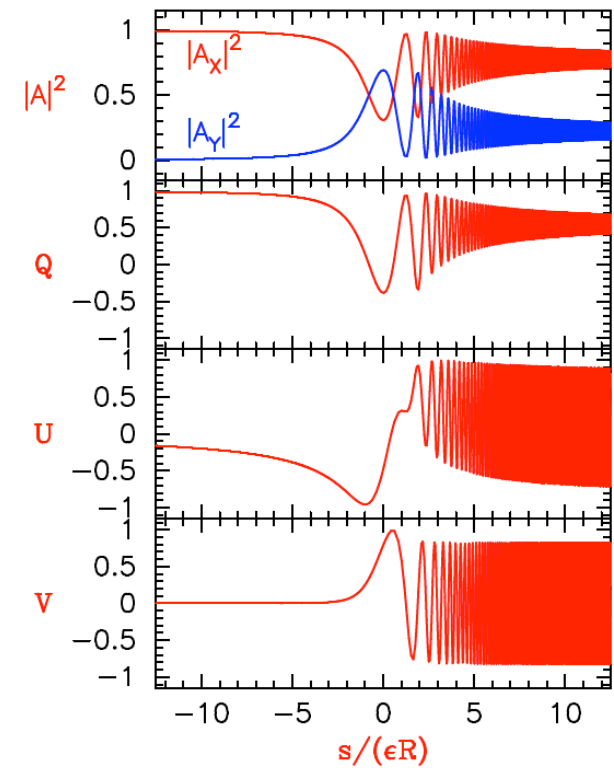
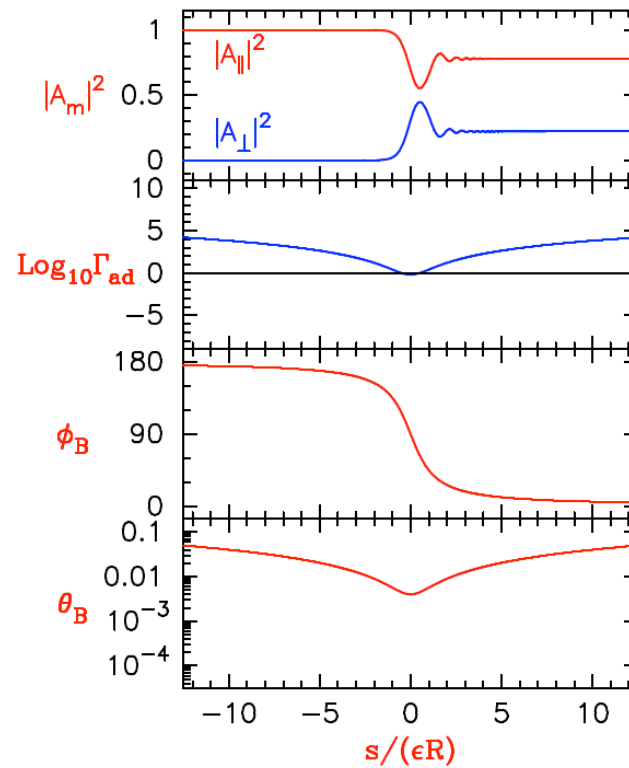
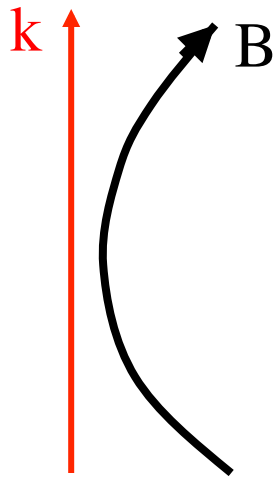
# Propagation of Polarization from NS Surface to Observer Through Magnetized Vacuum



polarization limiting radius  $\gg R$

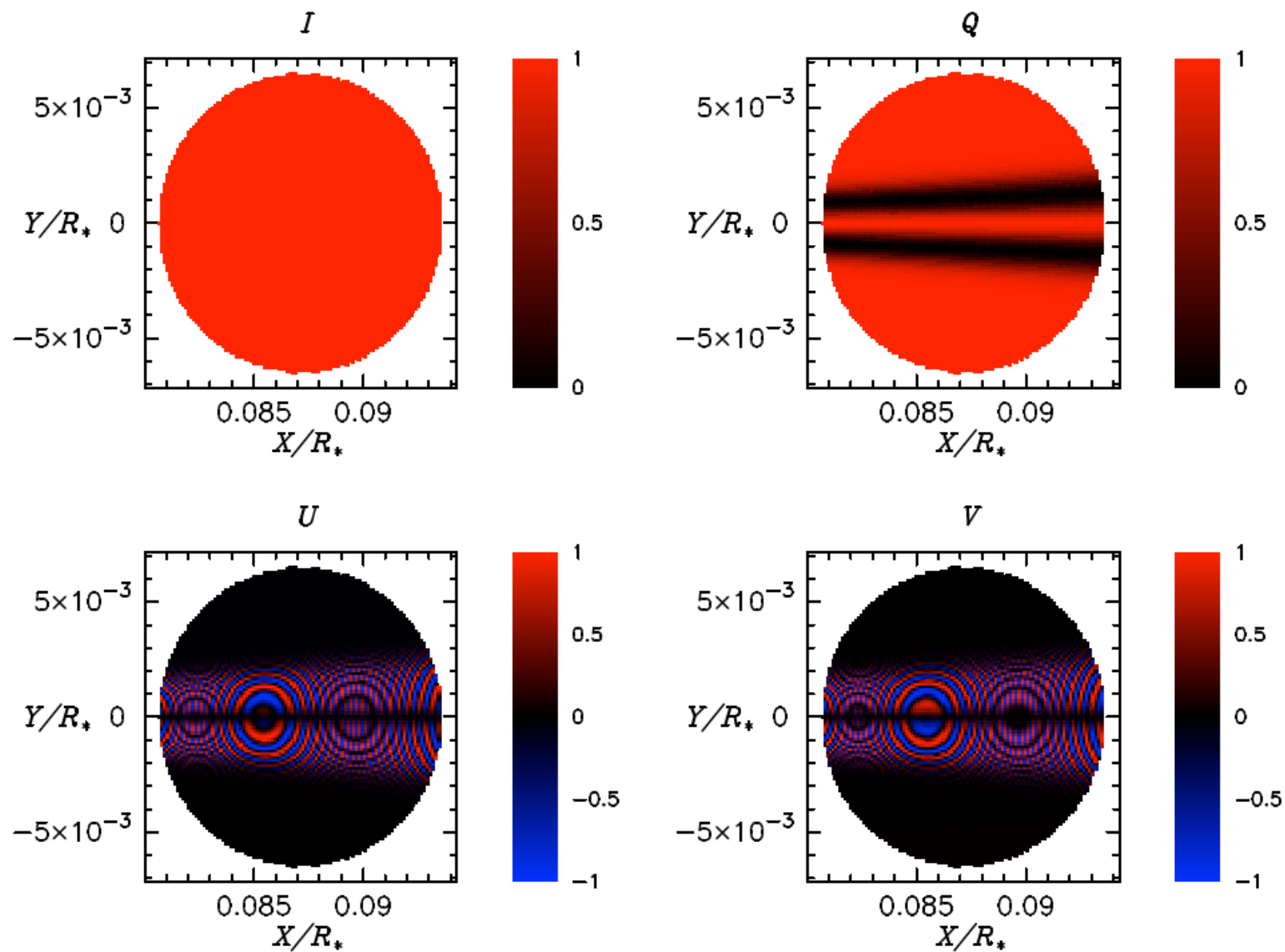
Polarization states of photons from different patches of the star are aligned at large  $r$ , and (largely) do not cancel --- Thanks to QED!

## But... Propagation through quasi-tangential region

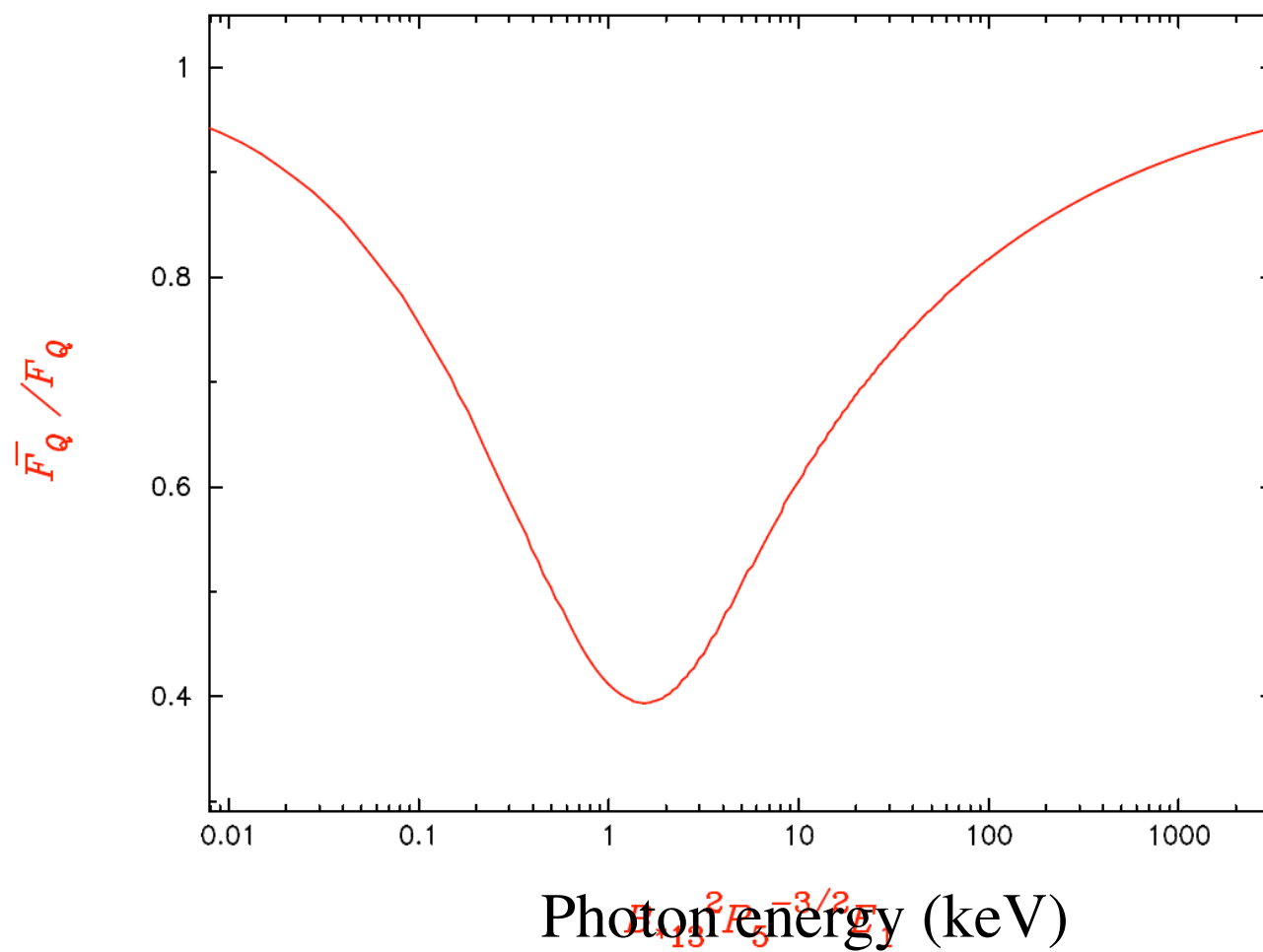


Wang & DL 2009

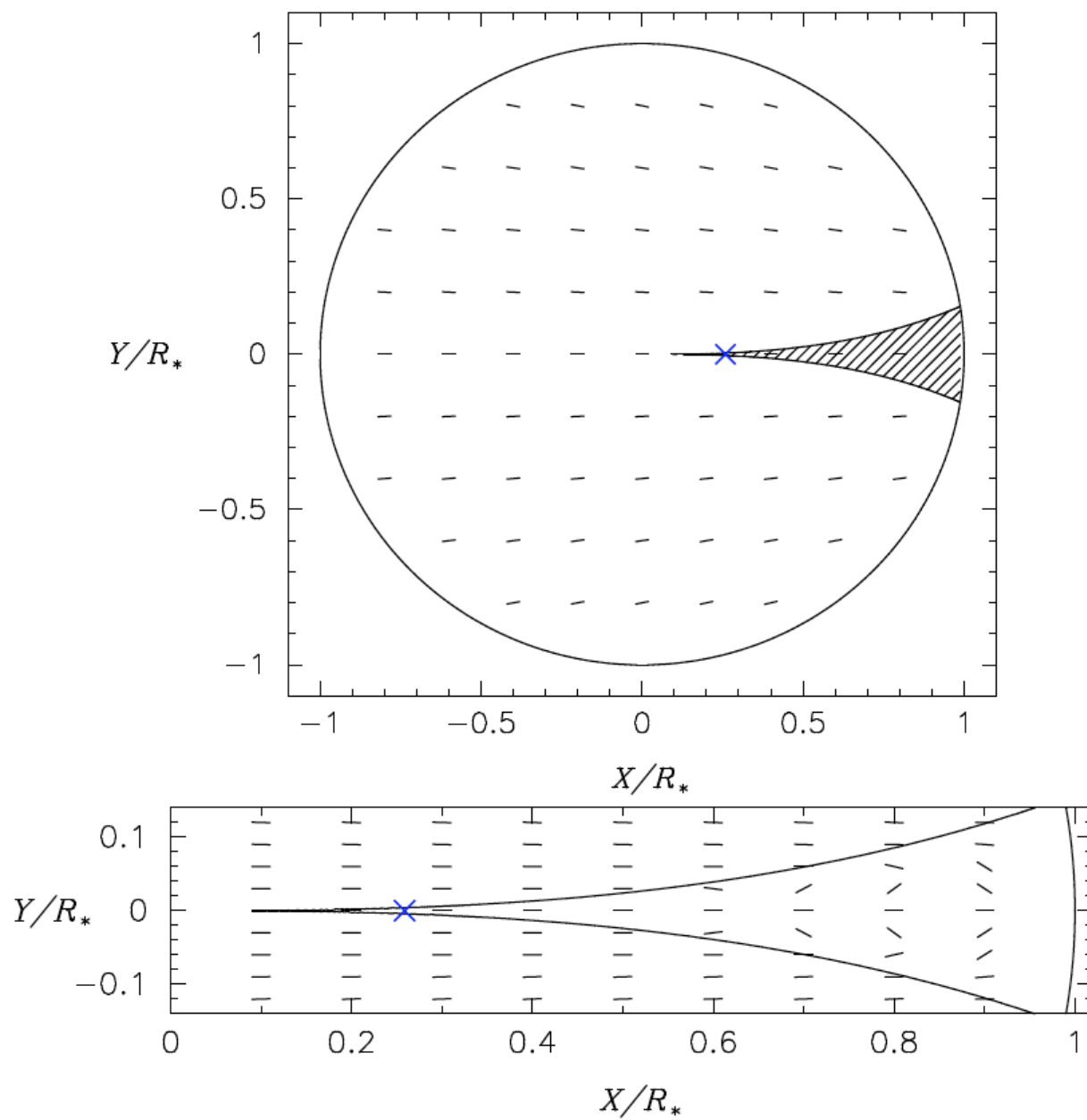
## Polarization map of polar cap (hot spot)



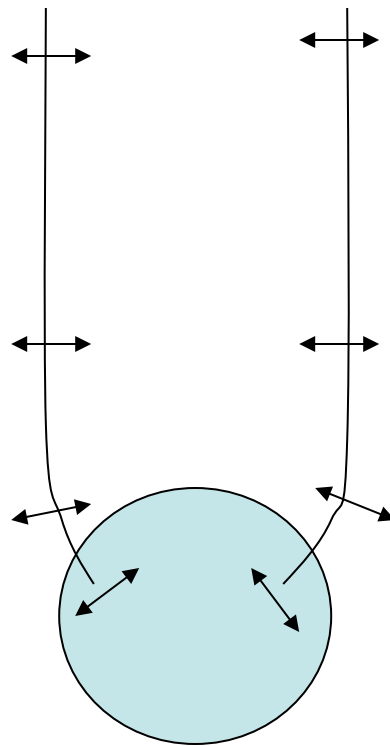
# Reduction of linear polarization due to quasi-tangential propagation



## Polarization map of the whole NS



# Propagation of Polarization from NS Surface to Observer Through Magnetized Vacuum



Polarization states of photons from **most** region of the NS surface are aligned at large  $r$ , and do not cancel --- Thanks to QED!

==>

Observed polarization direction depends only on the dipole component of the field, regardless of surface field structure.

(Recall: Intensity light curves depend on surface field structure)

# Summary

- Surface emission from magnetized neutron stars is highly polarized.
- X-ray polarization probes B-fields, geometry, beam patterns.  
Complementary to light curve and spectrum (polarization signal may still be interesting even when spectrum or lightcurve is boring.)
- Strong-field QED (vacuum polarization) plays an important role in determining the X-ray polarization signals:
  1. Gives rise to clean energy-dependent polarization signatures  
For  $B < 7 \times 10^{13} \text{G}$ , the plane of polarization at  $E < 1 \text{ keV}$  is  $\perp$  that at  $E > 5 \text{ keV}$ ;  
For  $B > 7 \times 10^{13} \text{G}$ , polarization planes coincide (but spectrum is affected).
  2. Aligns the polarization states of photons from different patches of the star so that net polarization remains large.

Probe strong-field QED.



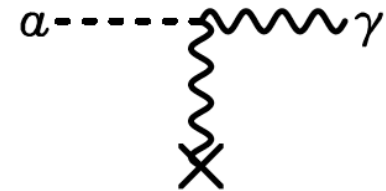
# Probing Axions with Magnetic Neutron Stars

# Probing Axions with Magnetic NSs

**Axions:** pseudoscalar particles, arise in the Peccei-Quinn solution of the strong CP problem; could be dark matter candidates (1980+)  
Recent motivation from string theory

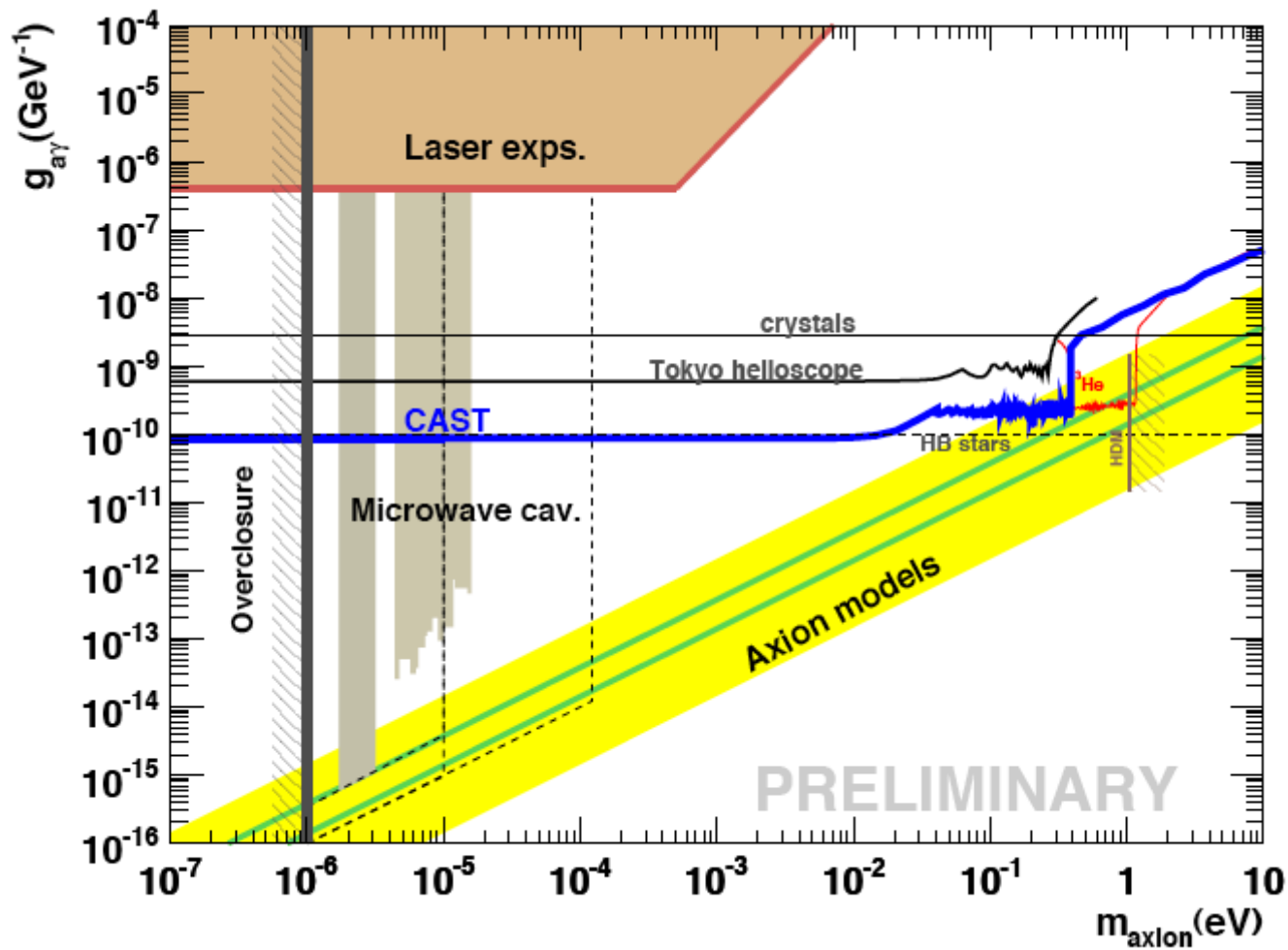
Can be produced or detected through the **Primakoff process**:

$$\mathcal{L}_{a\gamma} = -\frac{1}{4} g_{a\gamma} F_{\mu\nu} \tilde{F}^{\mu\nu} a = g_{a\gamma} \mathbf{E} \cdot \mathbf{B} a$$



**=>** //-component of photon can be coupled to axion

## Current constraints on axion mass and coupling parameter



# Photon-Axion Conversion in Magnetic Neutron Stars

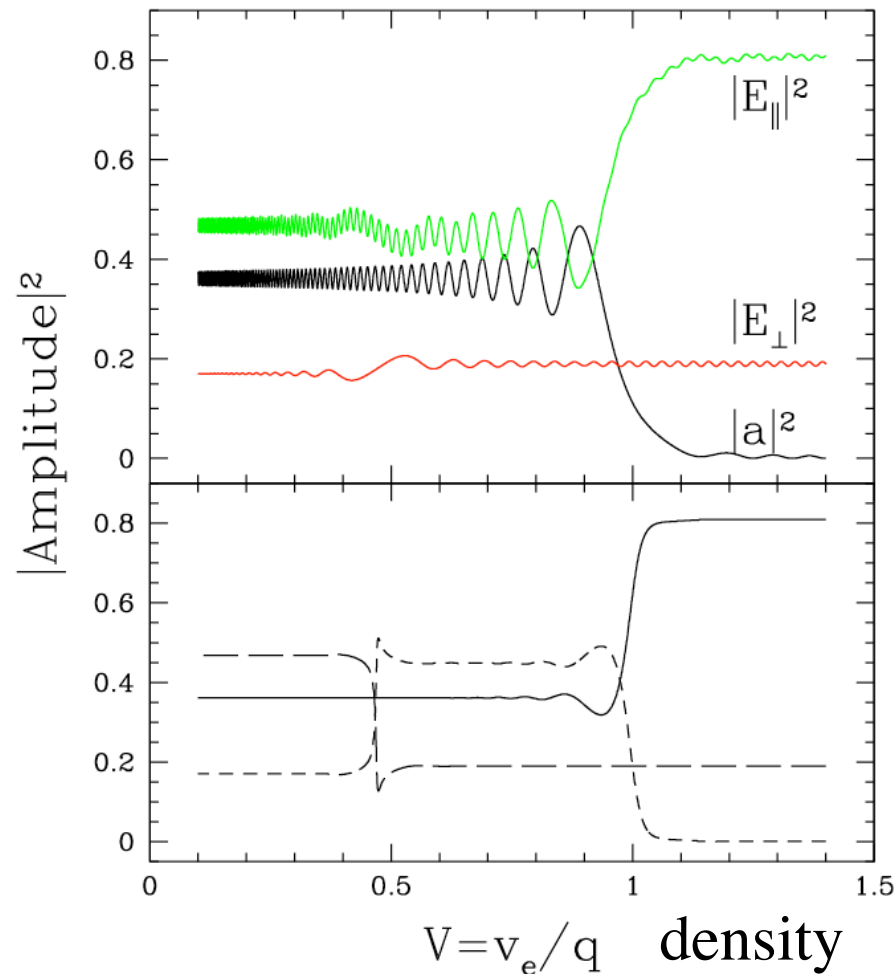
In the atmosphere and magnetized vacuum of NSs, photons (//-polarization comp) can convert into axions

**==> modify radiation spectra and polarization signals**

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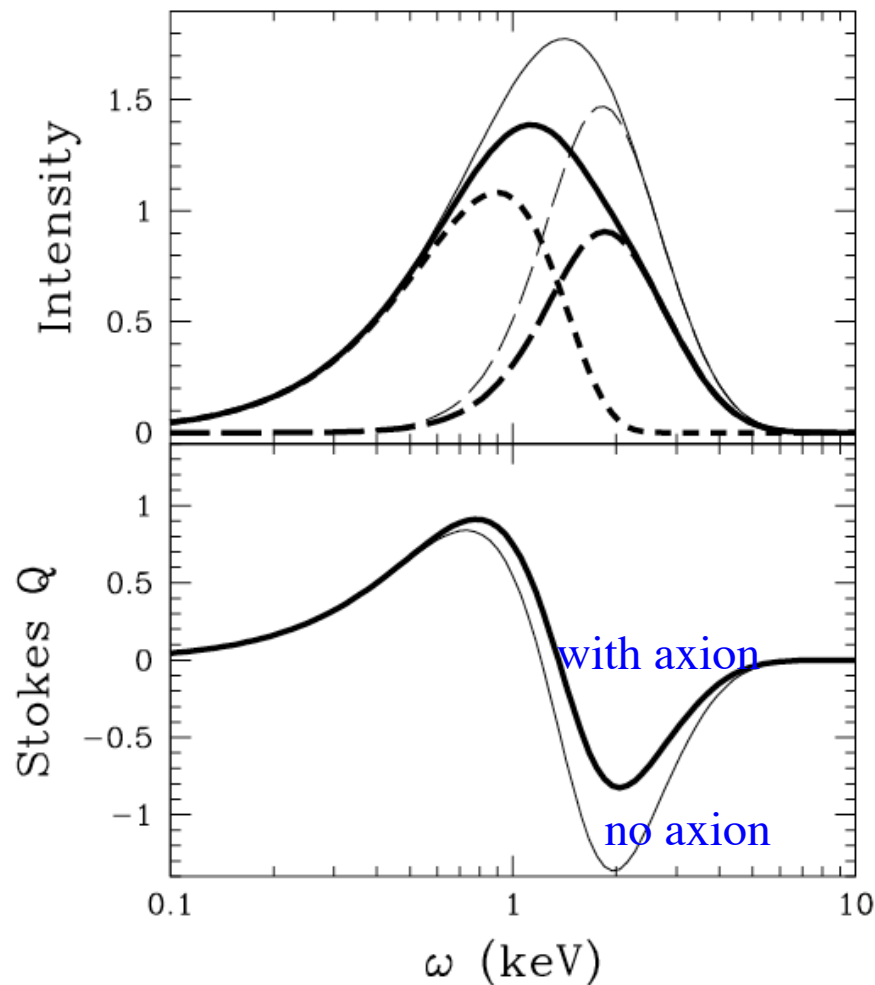
**==> modify radiation spectra and polarization signals**



# Photon-Axion Conversion in Magnetic Neutron Stars

In the atmosphere and magnetized vacuum of NSs, photons (//-polarization comp) can convert into axions

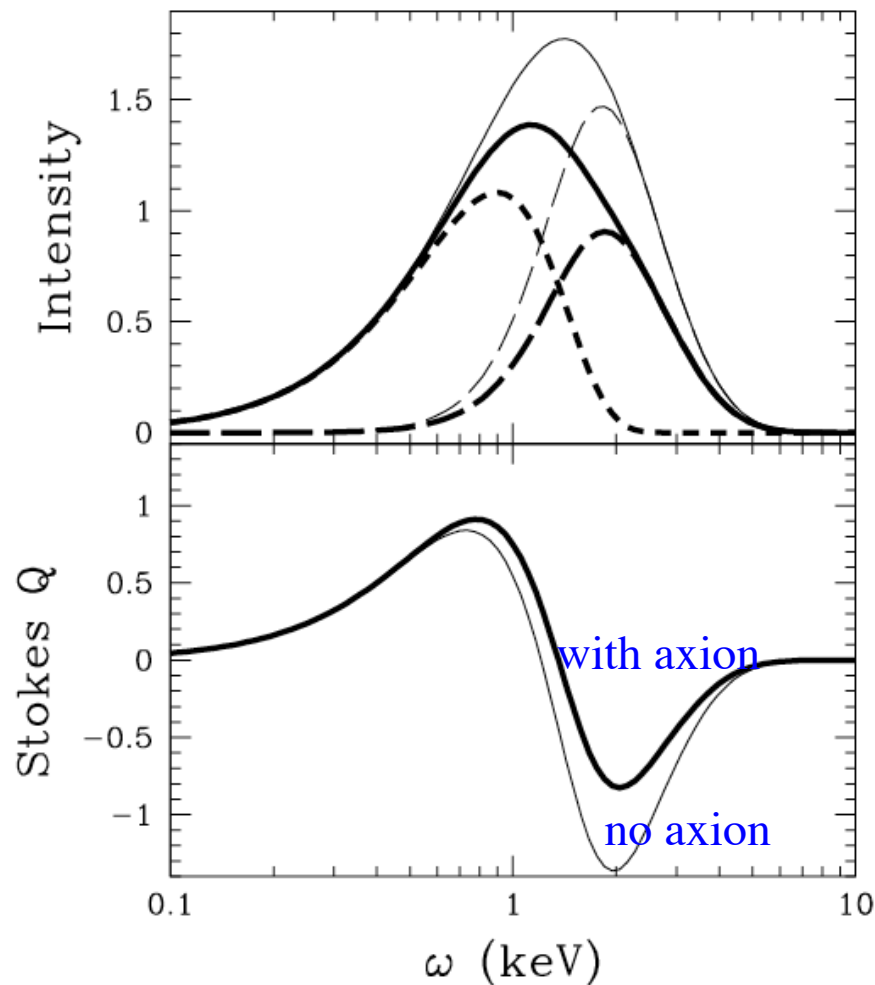
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# Photon-Axion Conversion in Magnetic Neutron Stars

In the atmosphere and magnetized vacuum of NSs, photons (//-polarization comp) can convert into axions

**==> modify radiation spectra and polarization signals**



Can in principle probe axions with parameters inaccessible by other experiments/constraints.

Unclear if we can separate out astrophysical uncertainty of the sources.  
(cf. Other indirect search of WIMPs)

Thank you!

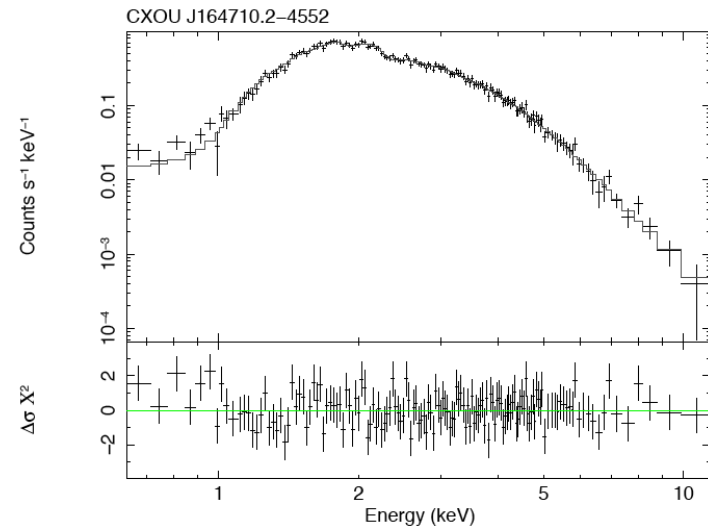


## Power-law emission of magnetars

- Likely due to resonant up-scatterings of surface photons by magnetosphere electrons/positrons (Thompson et al 2002; Fernandez & Thompson 2007)
- Magnetosphere charges (super-GJ) arise from twisting of field lines by crust (Thompson et al 2002; Beloborodov & Thompson 2007; Thompson 2009)

$$\nabla \times \mathbf{B} = \frac{4\pi}{c} \mathbf{J}, \quad n_e = J/(ec)$$

- Spectral modeling  
by Fernandez & Thompson 2007  
and Nobili et al 2008
- My guess is that the input polarization  
will be mostly perserved...





# Photon-Axion Conversion in Magnetic Neutron Stars

In the atmosphere and magnetized vacuum of NSs, photons (//-polarization comp) can convert into axions

====> modify radiation spectra  
and polarization signals

DL & Heyl 2007

